Target weight gain for moderately wasted children during supplementation interventions – a population-based approach

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Abstract

Objective: In malnourished populations, the weight-for-height Z-score (WHZ) distribution is shifted to the left. The aim of nutrition interventions should be to restore a normal WHZ distribution for the whole population. The present paper examines the WHZ change needed by each individual to achieve this objective.
Design: We developed a mathematical model of required individual change in WHZ as a function of characteristics of the initial population to restore a normal distribution. This model was then tested by simulating WHZ change needed to restore a normal WHZ distribution in a test population.
Setting: A rural area of Democratic Republic of the Congo with a high prevalence of undernutrition.
Subjects: Children under 5 years of age.
Results: To restore a normal distribution for the whole population, the WHZ of all children should be shifted. The desired WHZ change of each individual should be higher when the individual’s initial WHZ is low, when the mean WHZ of the whole population is low and, for the most wasted individual, when the variance of WHZ and WHZ change in the population are high. Using the suggested model in a simulation on the test population resulted in a WHZ distribution close to the growth standard.
Conclusions: To restore a normal WHZ distribution in wasted populations, nutritional programmes should cover the whole population with a higher weight gain in areas where mean WHZ is low.

Most programmes addressing moderate wasting with a weight-for-height Z-score (WHZ) between −3 and −2 discharge children when they reach a fixed threshold. This threshold is often set at a WHZ above −2 or −1. These fixed cut-offs have limitations. Reaching a WHZ of −2 may be too low for some children, who may initially have had a WHZ in the upper normal range and have entered the nutritional supplementation programme when they fell just below −2. These children might reach this discharge criterion with a small weight gain while still being substantially under their initial physiological weight. On the other hand, the −1 cut-off is not a good option either, as about 16% of the children in a normal well-nourished population are below this cut-off. Problems associated with the definition of wasting based on a fixed cut-off are also suggested by an observed mismatch between the clinical aspect of the child and his/her anthropometric status.

Another limitation of the current approach is that it assumes that only children below the arbitrary −2 Z-score cut-off are underweight and will benefit from nutritional supplementation. This is unlikely to be true. In a context of malnutrition, the whole WHZ distribution is usually shifted to the left, with a limited change in the variance of the WHZ distribution, indicating that all children are below their optimum WHZ. This situation indicates a sick population rather than only sick individuals, as described in another context.

Ideally, nutritional interventions should have the objective to restore the normal WHZ distribution in line with the WHO growth standards (WHZ mean = 0; WHZ SD = 1, WHZ variance = 1) which represents how a population of well-nourished children is supposed to grow. A population with a left-shifted WHZ distribution and an unchanged variance could be shifted back to a distribution like the growth standard with an intervention resulting in a uniform WHZ increase for all children across the WHZ distribution. This is unlikely to happen in real life, as WHZ increases during interventions have a great variability. For instance, in a recent supplementation study in moderately wasted children in Niger, the standard deviation of weight gain was comparable to weight gain itself.
The objective of the present study was to estimate the plausible WHZ change that each individual in a wasted population will need to restore the normal WHZ distribution in line with the WHO growth standards representing a well-nourished population.

Methods

The present paper first develops a mathematical model to estimate the individual's WHZ change that is needed during nutritional interventions to shift the WHZ distribution to the right to a standard deviation of 1 and a mean of 0. Further, a simulation is used to test the validity of this model.

Mathematical model

The average WHZ change needed to shift the whole distribution of WHZ to the right to get a new distribution with a mean of 0 and a standard deviation of 1 can be estimated using the relationship between the variance of a sum and the variance of each of its terms. The details of the calculation are given in the Appendix, where it is shown that the aimed WHZ change (ΔWHZ) for each child depends on his/her initial WHZ (WHZi), the mean and variance of the initial WHZ of the whole population before the intervention (Mean WHZ, Var WHZ), and the variance of ΔWHZ (Var ΔWHZ). These variables are linked by the relationships:

\[ f(x) = a + bx \]

and

\[ \Delta WHZ = a + b \cdot WHZ_i \]

with

\[ b = (1 - \text{Var WHZ}_i - \text{Var } \Delta \text{WHZ})/(2 \cdot \text{Var WHZ}_i) \]

and

\[ a = -\text{Mean WHZ}_i - b \cdot \text{Mean WHZ}_i \]

Simulation

The model above suggests that the average WHZ change needed to shift the distribution will depend on the variance of ΔWHZ. To estimate this variance, data from a longitudinal growth study of children from Democratic Republic of the Congo (DR Congo) were examined. That study took place in 1989–1991 and is described in detail elsewhere. In brief, a dynamic population including a nourished population, each child needed to increase his/her weight with an amount given by the regression model described above. To achieve the desired ΔWHZ variance, a random number was added to ΔWHZ for each child. The average of this added random number was 0, and thus this did not change the overall mean ΔWHZ. Its variance was the difference between the desired final variance (variance = 1) and the variance of change in WHZ observed after the addition of the ΔWHZ due to regression and before the addition of the random number. The resulting total variance of ΔWHZ was the desired variance.

Results

Estimation of variance of WHZ change

Among all the 3-months intervals, 3953 had an initial and a final WHZ which could be used to calculate the observed variance of ΔWHZ between visits. The variance for ΔWHZ for all these intervals was 0·63. This observed variance of ΔWHZ was used for the simulation.

Simulation of population shift

The mean WHZ in the baseline visit in the study population was −0·33 (variance 1·02). The change in WHZ that was needed to shift the WHZ distribution to a normal distribution with a mean of 0 and standard deviation of 1 was estimated with the model reproduced in the Appendix, assuming a variance of WHZ change of 0·63.

To restore the mean WHZ of 0 as expected in a well-nourished population, each child needed to increase his/her weight with an amount given by the regression model from his/her baseline WHZ as described in the Methods section and the Appendix. The WHZ change resulting from this WHZ increase due to regression had a variance of 0·10. To achieve the desired WHZ change variance, a random component with a mean of 0 and a variance of 0·53 was added. The resulting distribution is shown in Fig. 1. Mean Z-score after simulation was −0·01 (SD 1·02). The regression explained only a small fraction of WHZ change with an R² of 0·14, and simulated WHZ changes were highly variable even for the same initial WHZ (Fig. 2).
Even in this simulation which shifted the WHZ distribution to the right, some children lost weight in all WHZ categories. The proportion of children who lost weight among those with an initial WHZ less than $-2$ was 19.5% (Fig. 3).

**Discussion**

Mathematical analysis suggests that to restore a normal WHZ distribution in a population with an initial negative mean WHZ, interventions should in principle aim to change the WHZ of all children. This means that only nutritional programmes that have an effect on the growth of all children can restore a normal WHZ distribution. This is a strong theoretical argument for blanket, community-based nutritional interventions, rather than individual targeted interventions.

The practical implications of these findings should be considered carefully. The health benefits of restoring a normal WHZ distribution are unknown, and they may be small in relation to the costs in settings with a low...
prevalence of malnutrition. The relationship between anthropometric deficit and the risk of death is not linear but exponential\(^{(12)}\), suggesting that differences in WHZ status on the left part of the distribution are associated with higher number of deaths. In populations with a low prevalence of malnutrition, it may be more advantageous to target nutrition interventions to high-risk groups (i.e. with WHZ less than \(-2\)), as these are at an increased risk of mortality\(^{(13)}\). This analysis does not provide any information on the risk and benefits on morbidity and mortality of targeted vs. more universal interventions.

The present study suggests a different response to the same nutritional intervention depending on the initial mean WHZ deficit in the population, the highest WHZ change being required in populations with the lowest mean WHZ. In this respect, the highest weight gains for moderately wasted children have been reported from Niger, an area with a high prevalence of wasting\(^{(14)}\). This contrasts with the lower weight gains reported from Malawi where wasting is less common\(^{(15)}\). Although part of this difference may be related to different treatment protocols and admission criteria, this is consistent with the hypothesis of a higher weight gain to be expected in areas of high prevalence of wasting.

The model also suggests that the variance of WHZ in the whole population influences the needed WHZ change, an increased variance requiring a higher WHZ change in the left part of the WHZ distribution. It also suggests that the WHZ change to be expected will be influenced by the variance of WHZ change itself, which may also be influenced by ongoing interventions.

For practical purposes, the model suggests that the mean WHZ change of moderately wasted children should always be superior to the left shift of the mean WHZ of the population. The Appendix (section C) shows how to calculate the needed WHZ change in relation to initial individual WHZ using a simple spreadsheet calculation. When interventions are targeted, the average initial WHZ of targeted individuals should be entered in the model to calculate needed average WHZ change. Calculation of this average requires integrating WHZ up to the cut-off chosen for intervention. This has been done in the Appendix (section D) for a normal distribution and Z-scores between \(-2\) and \(-3\) which are commonly used in targeted interventions.

Despite its limitations, the present study has implications for the evaluation of programmes targeted to moderately wasted children. For children with moderate wasting (WHZ between \(-3\) and \(-2\)), the present analysis suggests that the needed WHZ change will depend on the WHZ of each individual child, but also on the mean WHZ of the whole population, and on the variance of the WHZ change in the population. This suggests that the expected WHZ change in wasted children will be context specific, in particular depending on the mean WHZ of the population.

This simulation also suggests that within a WHZ category, and even when an intervention is successful to shift the WHZ distribution, some wasted children may lose weight, especially if variance of WHZ change is high. It is important to keep in mind that it is hard to predict how individual children will respond to interventions, but the anthropometric effect on a group level should still be a good indicator of whether interventions work appropriately.

Our model suggests that the needed WHZ change for each individual is higher when the average WHZ of the whole population is low. This is consistent with the higher predictive value of diagnostic criteria when malnutrition prevalence is high and identification of those malnourished is imperfect\(^{(16)}\).

These proposed needed WHZ changes for wasted children are however tentative. Also, the shift towards a normal distribution is not the only criterion to consider.
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when estimating the desirable WHZ shift for targeted programmes. In particular, the risk of relapse and the risk of severe acute malnutrition during follow-up should also be considered.

To summarise, the present study shows that nutritional programmes should cover the whole population with a severity-based approach to restore a normal weight-for-height distribution in wasted populations, aiming at a higher a weight gain in areas where the mean WHZ is low.

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References


Appendix

Estimation of WHZ needed to shift WHZ distribution to the right to a final mean of 0 and standard deviation of 1

A. Calculation of average WHZ change (Mean ΔWHZ) for the whole population

To change the mean in a population to 0, the required change should be equal to the initial difference from 0:

\[
\text{Mean} \Delta \text{WHZ} = -\text{Mean WHZ}_i
\]

B. Calculation of average needed weight gain for a given WHZ

The variance of a sum can be calculated using the general formula:

\[
\text{var}(y) = \text{var}(x_1) + \text{var}(x_2) + 2 \cdot \text{covariance}(x_1, x_2)
\]

The variance of WHZ change (Var ΔWHZ), the variance of initial WHZ (Var WHZ_i) and the variance of the final WHZ (Var WHZ_f) are related as follows:

\[
\text{Var WHZ}_f = \text{Var WHZ}_i + \text{Var ΔWHZ} + 2 \cdot \text{Cov} (\text{WHZ}_i, \Delta \text{WHZ})
\]

The mean of WHZ should be 1 and its variance should be 1^2 = 1. Hence:

\[
1 = \text{Var WHZ}_i + \text{Var ΔWHZ} + 2 \cdot \text{Cov} (\text{WHZ}_i, \Delta \text{WHZ}) \quad \text{and}
\]

\[
\text{Cov} (\text{WHZ}_i, \Delta \text{WHZ}) = \frac{(1 - \text{Var WHZ}_i - \text{Var ΔWHZ})}{2}
\]

WHZ change in relation to initial WHZ can be calculated by the general equation for a linear regression model:

\[
\Delta \text{WHZ} = a + b \cdot \text{WHZ}_i
\]
with
\[
a = \text{Mean } \Delta \text{WHZ} - b \cdot \text{Mean WHZ}_i
\]
or
\[
a = -\text{Mean WHZ}_i - b \cdot \text{Mean WHZ}_i
\]
and
\[
b = \frac{\text{Cov}(\text{WHZ}_i, \Delta \text{WHZ})}{\text{Var WHZ}_i}
\]
or
\[
b = \frac{(1 - \text{Var WHZ}_i - \text{Var } \Delta \text{WHZ})}{2 \cdot \text{Var WHZ}_i}
\]

Figures A1, A2 and A3 show the relationship between WHZi and needed ΔWHZ for different mean WHZi values for the whole population, for different variances of ΔWHZ and for different variances of WHZi of the whole population.

C. Calculation of WHZ change needed in relation to the parameters of the initial population and expected WHZ change variance with a standard spreadsheet

(i) Data entry spreadsheet
Population data
- Mean WHZ: B5
- Variance WHZ: B6
- Variance of WHZ change: B7
Individual data
- Initial WHZ: B11

(ii) Calculations
Slope: B15 = \((1 - B6 - B7)/(2*B6)\)

(iii) Results
- Intercept: B17 = B5 - B15*B5
- Expected WHZ change for individual: B21 = B17 + B11*B15

This calculation can be made on several columns for different values of initial WHZ for individuals to reproduce plots as in Figs A1 to A3.

D. Average WHZ for children with a WHZ between \(-2\) and \(-3\) in relation to the average WHZ of the population

<table>
<thead>
<tr>
<th>Initial mean WHZ of the population</th>
<th>Average WHZ of children between Z-score of (-3) and (-2)</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.0</td>
<td>-2.32</td>
</tr>
<tr>
<td>-0.1</td>
<td>-2.32</td>
</tr>
<tr>
<td>-0.2</td>
<td>-2.33</td>
</tr>
<tr>
<td>-0.3</td>
<td>-2.33</td>
</tr>
<tr>
<td>-0.4</td>
<td>-2.34</td>
</tr>
<tr>
<td>-0.5</td>
<td>-2.35</td>
</tr>
<tr>
<td>-0.6</td>
<td>-2.35</td>
</tr>
<tr>
<td>-0.7</td>
<td>-2.36</td>
</tr>
<tr>
<td>-0.8</td>
<td>-2.37</td>
</tr>
<tr>
<td>-0.9</td>
<td>-2.38</td>
</tr>
<tr>
<td>-1.0</td>
<td>-2.38</td>
</tr>
</tbody>
</table>

These values were calculated assuming a variance of 1 for the WHZ distribution in the population. These values should be used in the model above (cell B11) to calculate the average WHZ change needed for children between Z-scores of \(-2\) and \(-3\).

Fig. A1 Change in weight-for-height Z-score (WHZ) needed to restore a normal distribution in relation to the initial WHZ for different values of mean initial WHZ (- - - - - , Mean WHZ = -0.7; -----, Mean WHZ = -0.5; ----, Mean WHZ = -0.3; ---, Mean WHZ = 0). When the mean WHZ in the population is 0, children in the lower range of WHZ are on average expected to increase WHZ whereas the children in the upper range are expected to decrease their WHZ, in accordance with the principle of regression to the mean; when the mean WHZ is negative, children in all WHZ ranges should have a mean WHZ change above what is needed when the mean initial WHZ is 0.
Fig. A2 Change in weight-for-height Z-score (WHZ) needed to restore a normal distribution in relation to the initial WHZ for different values of variance of WHZ change (---, Var \( \Delta \text{WHZ} = 0.5 \); ----, Var \( \Delta \text{WHZ} = 0.6 \); ---, Var \( \Delta \text{WHZ} = 0.7 \)). When variance of WHZ change increases, the regression to the mean is increased. As a result, WHZ gain needed for wasted children increases and children with the highest WHZ should decrease their WHZ.

Fig. A3 Change in weight-for-height Z-score (WHZ) needed to restore a normal distribution in relation to the initial WHZ for different values of variance of WHZ in the initial population (---, Var WHZ\(_i\) = 0.7; ----, Var WHZ\(_i\) = 1.0; ---, Var WHZ\(_i\) = 1.3). When overall variance of WHZ in the initial population increases, higher WHZ gains are needed for wasted children.