



## Full Length Article

# Compressional wave phase velocity measurements during hydrate growth in partially and fully water saturated sandstone

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## ABSTRACT

The compressional wave phase velocity ( $c_p$ ) has been measured as a function of hydrate saturation ( $S_H$ ) during hydrate growth in Bentheim sandstone. The Fourier spectrum signal processing technique was used to specifically obtain the phase velocity at frequency 500 kHz. Eight experiments were conducted on eight Bentheim sandstone samples, having initial water saturation ( $S_{wi}$ ) in the range 0.51–1. Based on the measurements, it is discussed how  $S_{wi}$  might affect the hydrate formation pattern during hydrate growth. For the sample having  $S_{wi} = 0.51$ , a clear increase is observed in the measured  $c_p$  from the beginning of the hydrate formation process. In the literature, micropore models ascribe such an increase to hydrates partly forming in soft, low aspect-ratio pores. For the samples having  $S_{wi} \geq 0.68$ , there is an initial stage in the hydrate formation process with little or no change in the measured  $c_p$ . The  $S_H$  interval defining this first stage seems to increase for increasing  $S_{wi}$ . As  $S_H$  further increase, a second stage follows where  $c_p$  increases. This is explained with hydrates first forming as a hydrate-water slurry before eventually solidifying and taking part of the solid frame. The results aid in understanding how the elastic properties of hydrate-bearing porous rocks change with  $S_H$  and  $S_{wi}$ .

## 1. Introduction

Vast quantities of methane gas hydrates stretch over large volumes beneath the ocean-bed, inland seas, and in the permafrost, and may potentially become an energy source [1,2]. In hydrate-bearing sediments, the hydrate saturation ( $S_H$ ) may typically be related to the compressional ( $c_p$ ) [2–15] and shear ( $c_s$ ) wave velocities [2,3,6–8,12,13], and the compressional ( $\alpha_p$ ) and shear ( $\alpha_s$ ) wave attenuation coefficients [2,7,9]. Thus, acoustic methods have been pointed to as candidates for remote detection and monitoring of hydrate deposits [1,2].

In addition to  $S_H$ , and confining pressure, the acoustic parameters  $c_p$ ,  $c_s$ ,  $\alpha_p$ , and  $\alpha_s$  of hydrate-bearing poroelastic solid media depend on many other factors. The pore fluid, which is typically described with the gas ( $S_g$ ) and water ( $S_w$ ) saturations clearly affect  $c_p$  and  $c_s$  along with sediment composition in standard rock physics models such as Gassmann's equation [16]. The measurement frequency will affect all the acoustic parameters due to dispersion and attenuation mechanisms [15,17], and from laboratory studies the hydrate morphology is reported to have a clear effect on  $c_p$  and  $c_s$  [4–6,8,11–13]. Information on how these listed factors affect the acoustic parameters are needed to

understand acoustic field measurements [2,3,7,18].

By interpreting the measured  $c_p$  and  $c_s$  using numerical models it has been investigated whether hydrates form primarily within the pore fluid, or hydrates take part in the solid frame. For unconsolidated sediments, numerical models distinguish between hydrates acting as load bearing grains [19] or as cement in between the grains [20]. Cementing hydrates greatly affects  $c_p$ . Hydrates acting as load bearing grains and hydrates forming in the pore fluid has some effect, and little or no effect, respectively, on  $c_p$ .

The differential effective medium model (DEM) is regarded as suitable for modeling  $c_p$  in consolidated sandstones. In this model, hydrates take part in the solid frame by filling up the pores which is described with spheroids having different aspect ratios [16]. Cementing effects in sandstones are typically regarded as solid material filling up the low aspect ratio pores [22].

Zhang et al. [11] studied the hydrate morphology during hydrate growth in unconsolidated sand for a range of initial water saturations (approximately 0.15 – 0.70). Hydrate forming in the samples in the lower water saturation range, was reported to mainly act as cement between the grains. For samples in the intermediate to high water saturation range, a combination of all three hydrate morphology

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scenarios was used to describe the change in  $c_p$  during hydrate growth. Hydrate tended to form, primarily within the pore fluid early in the hydrate formation process,  $S_H$  typically less than 0.1, and act as load bearing grains for  $S_H$  typically in the range of 0.1 – 0.2, and act as cement for  $S_H$  typically higher than 0.2.

In a study by Hu et al. [8], an artificial consolidated porous ceramic material having  $S_{wi} = 1.0$  and baseline compressional wave velocity ( $c_p$  at  $S_H = 0$ ) approximately 4250 m/s, was subject to methane hydrate growth. Hydrates were reported to, form in the pore fluid for  $S_H$  less than 0.3 and, form as part of the solid frame for  $S_H > 0.3$ .

Sadeq et al. [23] formed synthetic hydrate (THF) in Bentheim sandstones. The samples were initially fully saturated with a solution of 15 % THF and 85% water.  $c_p$  was measured as a function of time and reported to increase from approximately 3450 m/s at baseline condition to 3850 m/s at maximum hydrate saturation. A confining pressure of 14 Mpa was used. The measured  $c_p$  was observed to not change at the start of the hydrate formation process. It was argued that this was due to hydrates forming in the pore fluid.

Both sonic (typically less than 30 kHz) [6,9] and ultrasonic frequencies (typically higher than 100 kHz) [4,5,8,10,11,13] have been used to study elastic wave velocities in methane hydrate bearing sediments in the laboratory. As pointed out by Priest et al. [6], for hydrate-bearing sediments, elastic velocity measurements using ultrasonic frequencies are typically higher compared with those obtained from seismic data due dispersion mechanisms. Theoretical models considering Biot flow and acoustic scattering in hydrate bearing sediments have been developed to understand dispersion mechanisms for a wide range of frequencies [15,17]. To use such models the specific measurement frequency must be specified, which is typically not done in studies where ultrasonic frequencies have been used [4,5,8,10,11,13].

In studies where ultrasonic measurement frequencies have been used,  $c_p$  and  $c_s$  have traditionally been obtained by measuring the transit time of the first arrival of the acoustic pulse transmitted through the hydrate-bearing samples [4,5,8,10,11,13]. The accuracy of this measurement method has been debated in e.g [24], especially for use with porous media. In this study it is argued that the first arrival of the signal may be partly buried in noise, and for very high attenuation the whole first cycle may be difficult to detect. In addition, the frequency content of the transient of the signal is not defined, therefore, measurements of wave velocities using the first arrival of the signal must be regarded as a measure of the group velocity, and not the phase velocity [24]. To overcome such challenges, the Fourier spectrum signal processing method [25] may be used to measure the compressional wave phase velocity. Using the Fourier method, any recording of a finite pulse is a measure of the average properties of the medium in which the pulse travels through. Due to the defined frequency, measurements using this method may also provide valuable data for verification of numerical models considering dispersion.

To interpret seismic field data from hydrate-bearing sediments, the hydrate morphology and its relation to  $c_p$  is a key area of interest. To aid in understanding this relation, unconsolidated sand-pack samples have been used to facilitate hydrates [4–6,11,26–28], and to represent hydrate-bearing sediments occurring in the nature. In several studies, consolidated porous media have also been used to facilitate methane hydrates [8,12] and synthetic hydrates (tetrahydrofuran, THF) [23,29,30] to aid in understanding how  $c_p$  is affected by complex mechanisms in hydrate bearing reservoirs. Potential grain migration during hydrate growth [31] may also pose an increased level of complexity when using unconsolidated sand as the host sediment. By using a rigid consolidated sandstone with a relatively uniform pore size distribution, such as Bentheim sandstone, the complexity of the measurement system may be reduced. In the current work, Bentheim sandstone was used as the host sediment. Due to the uniformity of the sandstones, different cores are assumed to be comparable in terms of measured  $c_p$  for the same initial conditions, such as initial water saturation,  $S_{wi}$ .

There are quite a few laboratory studies on the acoustic properties of hydrate bearing sediments, e.g. [4–6,8,10–13,23,26–30]. Few of these mentioned studies report measurements of  $c_p$  during hydrate growth over a wide initial water saturation ( $S_{wi}$ ) range [11,26]. As pointed out in [26], more published data will aid in understanding the complex mechanisms in hydrate bearing reservoirs, and also provide valuable input parameters to numerical models aiming to relate e.g.  $c_p$  and  $S_H$ .

The objective of the present work is to study the relation between hydrate growth pattern and phase velocity,  $c_p$ , in Bentheim sandstone for initial water saturation,  $S_{wi}$ , over a wide range, 0.51 – 1. A consolidated sandstone was used as host material to reduce the complexity compared with a typical unconsolidated hydrate bearing system found in nature, where e.g. grain migration during hydrate growth might occur [31]. In particular, the aim is to relate the sole impact of hydrate growth on  $c_p$  to the hydrate growth pattern for  $S_{wi}$  in the range 0.51 – 1. The Fourier spectrum signal processing method is used to obtain the phase velocity  $c_p$  at 500 kHz.

## 2. Sample preparation and experimental procedure

### 2.1. Sample preparation

Hydrates were formed in the pore space of a high porosity, highly permeable sandstone acquired from the Bentheim quarry in Lower Saxony, Germany. The Bentheim sample used in these experiments had a porosity ( $\beta_0$ ) of approximately 23% and a permeability of 1–2 D, and was characterized by uniform pore geometry with an average pore diameter of 125  $\mu\text{m}$ . This outcrop rock has been characterized by 95.5 % quartz, 2.0% kaolinite, 1.7% K-feldspar, and 0.8% other [32]. Bentheim sandstone has very low clay content [33] and no clay swelling has been observed in the current work. Eight individual cylindrical core plugs cut from the same batch were prepared with diameter 50.8 mm and different lengths ( $L$ ) (Table 1). The core plugs were dried at 70 °C for 24 h to remove all moisture and the dry weight was recorded. Each core plug was saturated with a given amount of water by one of two different methods [35,38]. In method (i), the dry core plugs were submerged in water for some time to allow water to invade the pore space by spontaneous imbibition at ambient conditions. The submerging time for the core in experiment 1 was 10 min; for experiments 2–3, two hours; for experiment 4–6, 24 h. In method (ii), the dry core plugs were first purged in a vacuum chamber (less than 1000 Pa) for two hours. The cores were then completely saturated by opening a valve to a secondary chamber containing water at ambient conditions. A standardized slightly saline water solution available at the laboratory facility was used as the water phase, containing distilled water with 0.1 wt% NaCl. Two of the core plugs were saturated by method ii), while the others were saturated by method i) (Table 1). The average initial water saturation,  $S_{wi}$  ( $S_w$  before hydrate growth), was calculated by the weight difference of the wet and dry core. Table 1 shows  $S_{wi}$ , saturation method, sample length ( $L$ ), porosity, and figures giving the corresponding measurements.

The sensitivity of  $S_{wi}$  in the cores based on uncertainties in the

**Table 1**

The experiment numbers (Exp. No.) are listed from low to high  $S_{wi}$  saturation method (cf. text), sample length ( $L$ ), porosity, and figures giving the corresponding experimental results.

Exp. No.	$S_{wi}$	Saturation method	$L$ [mm]	Porosity ( $\beta_0$ )	Figure
1	0.51	i)	44.4	0.233	Figs. 4 and 7
2	0.68	i)	48.7	0.239	Figs. 4 and 7
3	0.72	i)	49.2	0.237	Figs. 4 and 7
4	0.77	i)	48.4	0.239	Figs. 5 and 7
5	0.80	i)	42.7	0.239	Figs. 5 and 7
6	0.82	i)	42.4	0.237	Figs. 5 and 7
7	1.00	ii)	37.9	0.229	Figs. 6 and 7
8	1.00	ii)	53.7	0.229	Figs. 6 and 7

measured mass and pore volume of the sandstone, is found to be less than 0.02, which is in agreement with [34]. A note must be made for experiments 7–8 where  $S_{wi}$  is reported to be 1. Here water drainage near the surface of the sandstone will give an effectively smaller  $S_{wi}$ , however, in the core,  $S_{wi}$  is assumed to be unity. NMR imaging of similar Bentheim sandstone cores has previously shown that saturation method (i) gives local variations of the water saturation in the length direction of approximately 0.02, and in the inner parts of the sandstone, a radial variation of approximately 0.07 [35]. No systematic water congestion due to gravity is reported. Although there is some spatial variation in the water saturation, the Fourier spectrum method measures the average properties of the sandstone.

## 2.2. Pressure cell setup and hydrate formation procedure

The experimental system consists of the sandstone core sample, a Hassler core holder [34] (Fig. 1) to maintain the sample at high pressure and low temperature, a high pressure control system (overburden), and a pump to supply methane and control the pore pressure.

The transducers and buffers placed inside two transducer holders were pressed onto the sample by applying a 10 Nm torque using a 30 cm long torque wrench on the endpiece. By assuming frictionless endpiece threads, this torque will give an axial stress on the Bentheim sandstone of approximately 0.3 Mpa. A plexiglas cup, rubber ring, and centralizing ring were used to keep the transducers, buffers, and the sample aligned (see [36] for more details). All flow lines leading into the core were purged under vacuum and filled with methane gas. Using a Stigma pressure pump, the core plug was subsequently pressurized from both ends to 8.3 Mpa. The confinement pressure was continuously kept at 3.0 Mpa above the pore pressure by applying pressurized confining oil (11.3 Mpa) around the rubber sleeve (see Fig. 1). This results in a confinement stress of approximately 3 Mpa, much higher than the axial stress from the buffers. The core plug was pressurized at room temperature up to several days to allow methane to equilibrate with the water. Afterwards, the leakage rate of the system was determined for all experiments 1–8 by logging the Stigma pressure pump volume for 24 h. The leakage rates in experiments 1–8 were observed to be less than 0.04 mL/hour which are deemed small for these kinds of experiments [34].

A temperature bath controlled the coolant temperature, which in turn was transferred to a cooling jacket surrounding the core holder shown in Fig. 1. The pressure and temperature were controlled and monitored by computers, which allowed the test to run unattended for extended periods of time.

Hydrate formation was initiated by cooling – well below the methane hydrate formation temperature: 11.2 °C, at pressure 8.3 Mpa, and salinity 0.1 wt% NaCl, as calculated using the CSMGem software [37]. The temperature was reduced by flowing cooled antifreeze fluid through a cooling jacket that surrounded the core holder (not shown in Fig. 1). Following this formation procedure, NMR imaging shows that hydrate may be formed inside sandstone samples with  $S_{wi}$  up to unity [38]. In experiments 7–8, where  $S_{wi}$  is reported to be 1, methane invades inner

pore spaces by dissolving into the water [38]. Hydrate formation from dissolved methane gas is a much more slow process than hydrate formation on the gas/water interface [39]. Thus, experiments 7–8 ( $S_{wi} = 1$ ) lasted for weeks and experiments 1–6, where free gas was available, lasted up to a few days. For each experiment, acoustic waveforms were logged continuously.

The hydrate saturation,  $S_H$ , was quantified by the amount of methane gas consumed during hydrate growth assuming a hydration number of 5.99, and leakage rates were corrected for as described by [40]. Throughout the hydrate formation process the pore pressure was maintained at 8.3 Mpa by the pressure pump. For all experiments the consumed methane gas was logged on a computer communicating with the gas pressure pump. Loggings may be found in [41].

Numerous experiments have been conducted using the Hassler core holder shown in Fig. 1 [34,35,38,40]. In different Bentheim sandstone samples using this specific Hassler core holder, the uncertainty in  $S_H$  due to uncertainty contributions from the pressure pump methane volume, hydration number, methane gas density, thermometer precision, fluctuations of temperature in the pressure pump, and leakage rate is reported to be less than 0.02 [34]. This reported uncertainty in  $S_H$  for hydrate-bearing Bentheim sandstone samples inside the Hassler core holder applies for experiments with a low leakage rate [34] which is indeed the case for the current experiments with leakage rates less than 0.04 mL/hour. A relatively uniform hydrate distribution has been reported for experiments like this [38], although the spatial variation in the water saturation will affect the uniformity of hydrate saturation.

## 2.3. Acoustic experimental setup

$c_p$  was measured using the buffer rod arrangement with the pulse-transmit acoustic measurement method [42]. Fig. 1 shows how transducers, buffers, and the specimen are fitted inside the pressure cell. The “transmitting electronics” in Fig. 1 are the equipment needed to generate the electric input signal for the transmitting transducer. This consist of an Agilent 33250A signal generator, an ENI 240L RF power amplifier, a 33 mH inductor, a Hatfield attenuator, and electrical cables. The attenuator was used to ensure and confirm that non-linear effects did not affect the measurements significantly. The 33 mH inductor was used as a simple impedance matching filter between the attenuator and the transmitting transducer. It was used to remove some of the reactance (imaginary part) of the impedance of the transmitted electrical signals.

“The receiving electronics” represents a Hewlet Packard signal amplifier, a Krohn-Hite 3202 bandpass filter, a 33 mH inductor used for impedance matching, a DPO 3000 Techtronix oscilloscope, and electrical cables. A computer was used to log the measured signals from the oscilloscope via USB connection, and to control the input settings on the signal generator via an IEEE 488 USB-GPIB adapter.

Two measurements are conducted when using the buffer rod method: Reference measurement A without the sample inserted (as shown in Fig. 1 without the sandstone), and measurement B with the hydrate bearing sample inserted into the wave propagation path (as shown in Fig. 1). Using the Fourier spectrum signal processing method,  $c_p$  is found by subtracting the phase of reference measurement A and measurement B. Doing this, time delays caused by the buffers, transducers, and other electric components in the measurements are automatically corrected for. The PC-controlled waveform input settings on the signal generator was a 1–2 cycles pulse, having center frequency 500 kHz and burst repetition rate 50 ms. The amplitude setting was dynamically changed as described in the experimental procedure below. A high-pass filter with a 200 kHz cut-off frequency was applied, to remove low frequency components. The oscilloscope acquired the signal by continuously averaging 256 measured signals. The acoustic waveform was logged every 15 min.

In the project funding this research, the idea was to measure both P and S-waves. P and S-wave transducers with center frequencies 530 and 460 kHz, respectively, were designed and build in-house to fit inside the

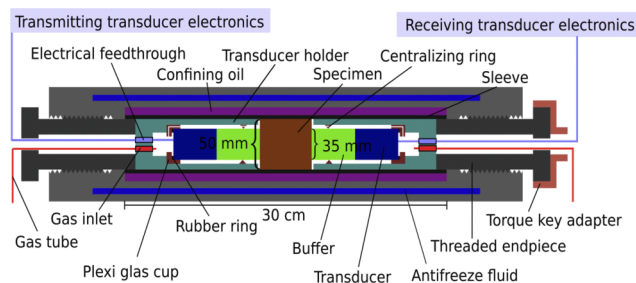


Fig. 1. Schematics of the pressure cell containing transducers, buffers, the hydrate-bearing sample, and other equipment needed for conducting acoustic and pressure cell regulation measurements.

pressure cell. However, S-waves were heavily attenuated in the experiments and mode conversion between S and P-waves may hamper the direct shear wave pulse. Thus only P-wave measurements are reported in this work. In experiments 1–3, the P-wave transducers were used and in experiments 4–8 the P-waves generated by the S-wave transducers were used. For further details on the design and construction of these transducers, cf. [36].

In a test measurement where the transducers were face to face (measurement A), a distorted signal was seen on the oscilloscope due to non-linear effects. To avoid this, the attenuator setting was set to 20 dB attenuation. No phase response was observed for the attenuator. In experiments 1–8 (measurement B), non-linear effects were avoided by gradually decreasing the signal generator amplitude from 100 mV to 1 mV during the measurements.

#### 2.4. Fourier spectrum signal processing technique

As pointed out in [43], the Fourier spectrum signal processing method [25] can be used in pulse-transmit measurements using the buffer rod arrangement to measure  $c_p$  for a porous rock. For precise ultrasonic measurements, the measured phase spectra should be corrected for diffraction effects [44]. By including the diffraction correction in the original method developed by [25],  $c_p$  has been obtained in this work with [36]

$$c_p = \frac{2\pi fL}{\angle V_A(f) - \angle V_B(f) + \angle H_B^{dif}(f) - \angle H_A^{dif}(f)}, \quad (1)$$

where  $f$  is the frequency.  $\angle V_A$  and  $\angle V_B$  are the discrete Fourier transform phase spectra of the P-wave pulses in measurements A and B, respectively.  $\angle H_A^{dif}$  and  $\angle H_B^{dif}$  are the diffraction correction phase spectra for measurement A and B, respectively, where  $H_A^{dif}$  and  $H_B^{dif}$  are the diffraction corrections.

Typical examples of the time traces using the S-wave transducer for measurements A and B are shown in Fig. 2. The first event in the time traces,  $A_P$  and  $B_P$ , are the direct transmitted P-wave pulses, which are used in this work.  $A_S$  and  $B_S$  are the direct transmitted S-wave events. Not clearly visible in the figure, however,  $A_S$  and  $B_S$  may be hampered by the other surrounding reflected S and P-wave events. Thus, shear waves are not considered in this paper.  $t_{AP}$  and  $t_{BP}$  are defined 10  $\mu$ s before the first peak in the pulse to ensure that potentially highly attenuated early signal components are included in the compressional wave event. Starting from  $t_{AP}$  and  $t_{BP}$ , the pulse is truncated after five cycles and zero-padded to a total signal length of 100,000 points (signal length 1 ms). The sampling frequency is 500 MHz and the frequency resolution of the Fourier spectrum is  $\Delta f = 1$  kHz. The FFT – algorithm in MATLAB 2017 is used to calculate the discrete Fourier transform. Using this algorithm, the phase spectra are wrapped within  $-\pi$  and  $+\pi$  and phase

jump discontinuities of  $2\pi$  will be present. Such phase jumps have been corrected for by adding  $2\pi$  at every discontinuity using the MATLAB 2017 function `unwrap()`. The Fourier spectrum signal processing technique is widely used for elastic velocity measurements, and more details on the method can be found in numerous studies, e.g [43]. A single event  $A_P$  or  $B_P$  (pulse) in Fig. 2 represents a wave with a wavefront covering (most of) the cross-section of the sample. Thus, the travel-time of the pulse gives information of the average properties of the sandstone, such as  $S_H$ . Thus, the Fourier method is suitable for measuring the average  $c_p$  in samples having some variation in properties such as hydrate and water saturation.

An expression derived by [45] has been used to calculate the diffraction correction for fluids and solids [46,47]. This approach has also been used in this work to calculate

$$\begin{aligned} H_A^{dif} &= 1 - e^{-i2\pi/Y_A} (J_0(2\pi/Y_A) + iJ_1(2\pi/Y_A)), \\ Y_A &= \frac{4\pi L_B}{k_b a^2}, \\ H_B^{dif} &= 1 - e^{-i2\pi/Y_B} (J_0(2\pi/Y_B) + iJ_1(2\pi/Y_B)), \\ Y_B &= \frac{4\pi L_B}{k_b a^2} + \frac{4\pi L}{k_m a^2}. \end{aligned} \quad (2)$$

Here,  $J_0$  and  $J_1$  are the first kind Bessel functions of the zeroth and first order, respectively and  $i = \sqrt{-1}$ .  $k_b = \omega/c_p^b$  and  $k_m = \omega/c_p$  are the compressional wave numbers in the buffer and the sample, respectively.  $c_p^b$  is the compressional wave velocity in the buffer and  $\omega$  is the angular frequency.  $L_B$  is the of the buffer length. In this work, using P-wave transducers, Eq. (1) has been used with “ $a$ ” equal to the piezoelectric element radius. For S-wave transducers, the piezoelectric elements are square shaped and  $a$  has been set to the radius of a circular disc with the same area as the square shaped element.

A rather thorough sensitivity analysis of uncertainty contributions in the measured  $c_p$  of experiments 1–8 can be found in [36] pp. 137–162. For the P-wave transducers (experiments 1–3), a combined sensitivity of  $c_p$  due to the uncertainties in diffraction correction, unwanted sidewall reflections in the acoustic experimental setup, repeatability, and sample length is estimated to less than 15 m/s using finite element simulations and reference measurements. The uncertainty contribution due to repeatability of the measurements is set to 11 m/s. By conducting measurements over several hours on a sample (without hydrate) placed within the pressure cell (Fig. 1), measurement results deviate less than 1 m/s. However, by conducting measurements and then decoupling and setting up the acoustic measurement setup again, measurements may deviate up to 11 m/s.

The absolute  $c_p$  is dependent on the repeatability of the measurements. During hydrate growth the transducers, buffers, and the sample are held in a fixed position and thus the repeatability of the change in  $c_p$  during hydrate growth is assumed to be much smaller than for absolute

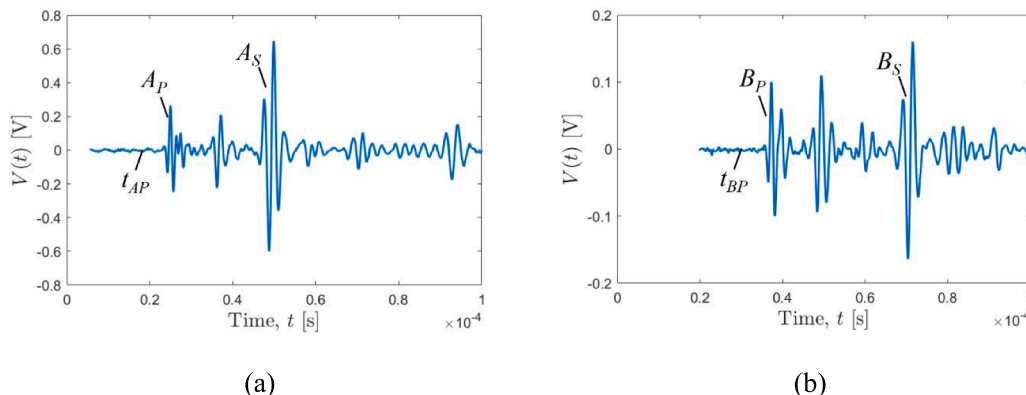


Fig. 2. Time traces for experiment 7 for  $S_H \approx 0.4$ . Events and first arrival transit times are shown for a) measurement A and b) measurement B.

measurements. This is clearly indicated by the repeatability measurements which change less than 1 m/s over time for a sample placed within the pressure cell. In general, measurements of the change in  $c_p$  are more accurate than the absolute  $c_p$  because hydrate growth in the core is assumed to have little or no effect on the listed uncertainty contributions, such as repeatability or sample length.

The sensitivity on  $c_p$  due to repeatability using S-wave transducers (experiments 4–8) is set to 45 m/s [36], however, the accuracy of the change in  $c_p$  during hydrate growth is assumed to be the same for the S and P-wave transducers.

### 3. Results

$c_p$  was measured for eight Bentheim sandstone samples (see Table 1) with different  $S_{wi}$  during hydrate growth using the buffer rod measurement method and Fourier spectrum method at 500 kHz. First the baseline velocity ( $c_p$  before hydrate growth,  $S_H = 0$ ) is presented, followed by measurements of experiments 1–8.

#### 3.1. Baseline velocity

In Fig. 3, measurements (blue x-markers) and calculations (red plus markers and black circles) of the baseline velocity as a function of  $S_{wi}$  are presented for the eight sandstone samples (Table 1). The DEM [21] is used to calculate the stiffness of the dry Bentheim rock frame, and Gassmann's equation [16] to include fluid effects. The fluid effects are calculated in two different ways; "Uniform": a uniform distribution of water and gas in the pores, and "Patchy": the water and gas are distributed separately in the sandstone [19]. Such effective medium models have been used for decades to describe properties of porous materials [16,19,21] and thus not repeated here. The relatively good agreement between measurements and calculations gives confidence in the acoustic measurement results and provides some insight in the initial water/gas distribution before hydrate growth.

The material properties used in the calculations are given in Table 2.  $K_w$ ,  $K_q$ , and  $K_g$  are the water, quartz, and methane gas bulk moduli, respectively.  $\rho_g$ ,  $\rho_q$ , and  $\rho_w$  are the methane gas, quartz, and water densities, respectively.  $\mu_q$  is the quartz shear moduli. The effective soft pore volume fraction,  $\alpha_1$ , and volume fraction,  $v_1$ , are obtained from Wang et al. [48] by interpolating between the reported values for Bentheim sandstone. The stiff pore volume fraction is  $v_2 = 1 - v_1$  and the stiff pore aspect ratio,  $\alpha_2$ , is set to 1, which is a typical value used for stiff pores [49,50] in sandstones. The porosities and initial water saturations from experiments 1–8 in Table 1 are used as input parameters.

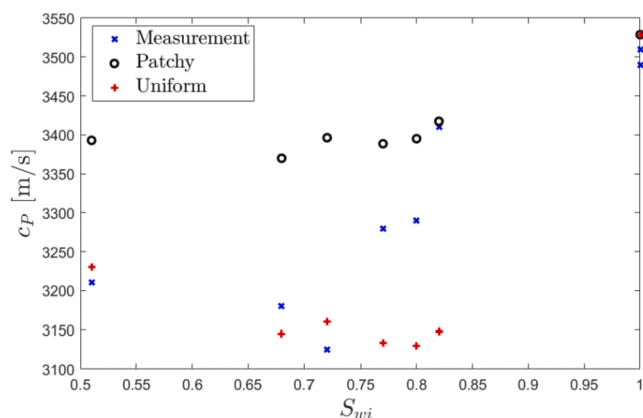


Fig. 3. Measurements (blue markers) and simulations of the baseline velocity ( $S_H = 0$ ) for experiments 1–8. The gas/water fluid mixture is modeled to either have a uniform or a patchy distribution. (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)

Table 2

List of material properties used in the simulations.  $K_g$  and  $\rho_q$  are calculated using the Peace Software [51] for temperature 4 °C and pressure 8.3 Mpa. The soft pore volume fraction,  $v_1$ , and soft pore aspect ratio,  $\alpha_1$ , are obtained based on the values reported in [48]. The stiff pore aspect ratio,  $\alpha_2 = 1$ , is taken as one of the typical values in [49]. The rest of the parameters are taken from Waite et al. [4].

Parameter	Value	Reference
$K_w$	2.25 Gpa	[4]
$K_q$	36.6 Gpa	[4]
$K_g$	11 Mpa	[51]
$\rho_g$	70 kg/m <sup>3</sup>	[51]
$\rho_w$	1000 kg/m <sup>3</sup>	[4]
$\rho_q$	2650 kg/m <sup>3</sup>	[4]
$\mu_q$	45 Gpa	[4]
$\alpha_1$	0,002	[48]
$\alpha_2$	1	[49]
$v_1$	0,023	[48]

In Fig. 3, the deviation between measurements (blue) and simulations where gas and water are uniformly distributed is less than 50 m/s for the samples having  $S_{wi} = 0.51, 0.57,$  and  $0.68$ . For the samples having  $S_{wi} = 0.77, 0.80,$  and  $0.82$ , a patchy gas distribution gives the best agreement. By comparing the measurements and simulations, there seem to be a transition from uniform to partially patchy gas distribution at approximately  $S_{wi} = 0.8$ . For experiments 6, 7, and 8, where  $S_{wi} = 0.82, 1,$  and  $1$ , respectively, a very good agreement is observed between the patchy distribution simulations and the measurements.

#### 3.2. Change in $c_p$ as a function of $S_H$ for experiments with $S_{wi}$ in the range 0.51–0.72

Fig. 4 shows the measurements during experiments 1, 2, and 3, where  $S_{wi}$  is 0.51, 0.68, and 0.72, respectively. In experiment 1 hydrates form quickly and  $c_p$  increases greatly with increasing  $S_H$  in the early stage of the hydrate formation process. The acoustic waveform is logged every 15 min and experiment 1 is thus better represented with markers than a continuous curve. (For experiments 2–8 the hydrate formation process is more slow and the datapoints are close enough to be represented with a continuous curve.) In experiment 1,  $c_p$  increases with approximately 800 m/s for  $S_H$  in the range 0–0.2, starting at  $c_p$  approximately 3200 m/s. For  $S_H = 0.4 - 0.6$ ,  $c_p$  flattens out.

In experiments 2 and 3,  $S_{wi}$  is 0.68 and 0.72, respectively, and the baseline  $c_p$  is approximately 3110 m/s and 3180 m/s, respectively. The curves for experiment 2 and 3 show a similar increase in  $c_p$  for increasing  $S_H$ . For  $S_H$  in the range 0 – 0.1, little or no change is observed in  $c_p$ . A very small decline might be indicated in this range. For  $S_H > 0.1$ , a clear increase in  $c_p$  is observed. At  $S_H = 0.5$  there is an increase of

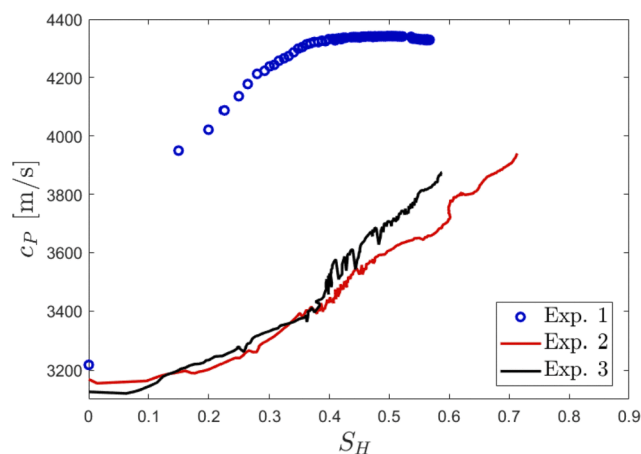


Fig. 4. Measured  $c_p$  as function of  $S_H$  for experiment 1 ( $S_{wi} = 0.51$ ), experiment 2 ( $S_{wi} = 0.68$ ), and experiment 3 ( $S_{wi} = 0.72$ ).

approximately 450 m/s and 550 m/s relative to the baseline velocity, in experiments 2 and 3, respectively.

The sensitivity analysis detailed in section 2.4 indicates an uncertainty in  $c_p$  of 15 m/s for results presented in Fig. 4.

As described in [52], hydrates may be redistributed during the dynamic hydrate formation process. This may explain the ripples observed for the measured  $c_p$  in Fig. 4. Such ripples are observed for experiments 4–8 as well, shown in Figs. 5–6.

### 3.3. Change in $c_p$ as a function of $S_H$ for experiments with $S_{wi}$ in the range 0.77–0.82

In Fig. 5,  $c_p$  is presented for experiments 4 ( $S_{wi} = 0.77$ ), 5 ( $S_{wi} = 0.80$ ), and 6 ( $S_{wi} = 0.82$ ). Data is missing for  $S_H$  in the range 0.27–0.62 in experiment 5 due to a crash on the computer logging the acoustic waveforms. The computer was restarted the next day, however as Fig. 5 shows, important information of  $c_p$  during the hydrate formation process is missing. A new experiment was then immediately planned with approximately the same  $S_{wi}$  as experiment 5. This new experiment is in fact experiment 6. The existing data from experiment 5 still give useful information on the hydrate formation process for  $S_H$  less than 0.25 and is thus included in Fig. 5. The baseline  $c_p$  is approximately 3270 m/s in experiments 4 and 5, and 3400 m/s in experiment 6. In all three experiments there is some initial decline in the measured  $c_p$  for low  $S_H$ . After this decline,  $c_p$  increase and is measured to be higher than the baseline  $c_p$  from  $S_H$  approximately 0.1–0.15. The increase in  $c_p$  from the baseline velocity to  $S_H = 0.5$  is approximately 500 m/s and 300 m/s, in experiments 4 and 6, respectively. For  $S_H > 0.5$ , the increase in  $c_p$  is higher for experiment 4 compared with experiment 6. The curve for experiment 5 flattens out and no change can be seen in the measured  $c_p$  for  $S_H > 0.6$ .

The sensitivity analysis detailed in section 2.4 indicates an uncertainty in  $c_p$  of 45 m/s for the results reported in Fig. 5. The change in  $c_p$  during hydrate growth, i.e. relative to the baseline velocity is set to 15 m/s.

The measured baseline velocity ( $S_H = 0$ ) in experiment 4 lies in between the “Uniform” and “Patchy” simulations in Fig. 3, indicating that there might be some regions in the sandstone having a patchy gas/water distribution.

The black curve for experiment 6 is approximately 100 m/s higher than for experiment 4 and 5. This may be partly explained by the slight difference in porosity (Table 1), between the cores in experiment 6, and experiments 4–5. Also, by comparing the simulated and measured baseline velocities in experiments 4–6 (Fig. 5), water and gas are indicated to be distributed in patches, especially in experiment 6. A patchy saturation will give a higher  $c_p$  than a uniform water/gas distribution.

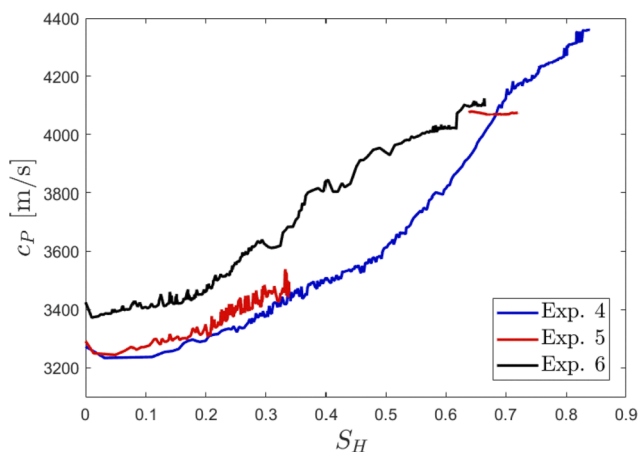


Fig. 5. Measured  $c_p$  as function of  $S_H$  for experiment 4 ( $S_{wi} = 0.77$ ), experiment 5 ( $S_{wi} = 0.80$ ), and experiment 6 ( $S_{wi} = 0.82$ ).

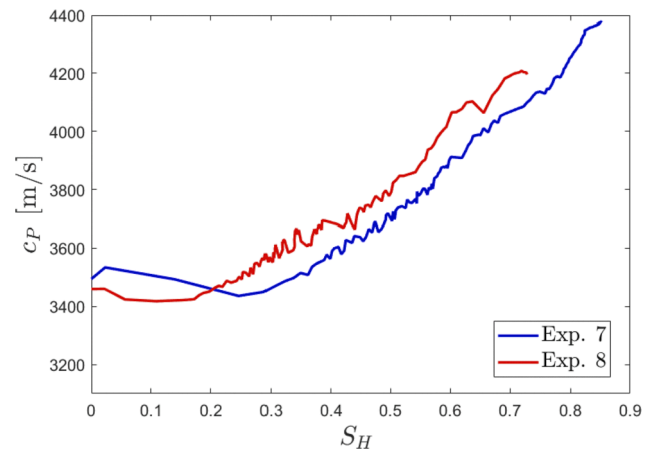


Fig. 6. Measured  $c_p$  as function of  $S_H$  for experiment 7 ( $S_{wi} = 1$ ) experiment 8 ( $S_{wi} = 1$ ).

### 3.4. Change in $c_p$ as a function of $S_H$ for experiments with fully water saturated samples

In Fig. 6, the measured  $c_p$  is presented for experiments 7 and 8, where  $S_{wi} = 1$ . The curves indicate an increase followed by a decrease in the measured  $c_p$  for low  $S_H$ . The “main” increase in  $c_p$  starts at  $S_H$  approximately 0.18 and 0.25 for experiments 7 and 8, respectively. The increase in  $c_p$  at  $S_H = 0.5$  relative to the baseline is approximately 200 and 300 m/s in experiments 7 and 8, respectively.

As seen in Fig. 3, for  $S_{wi} = 1$ , the measured baseline  $c_p$  is lower than the simulated baseline  $c_p$ . This deviation might be explained if there are small amounts of gas still present in the pores, which is not accounted for in the simulations, where  $S_{wi} = 1$ .

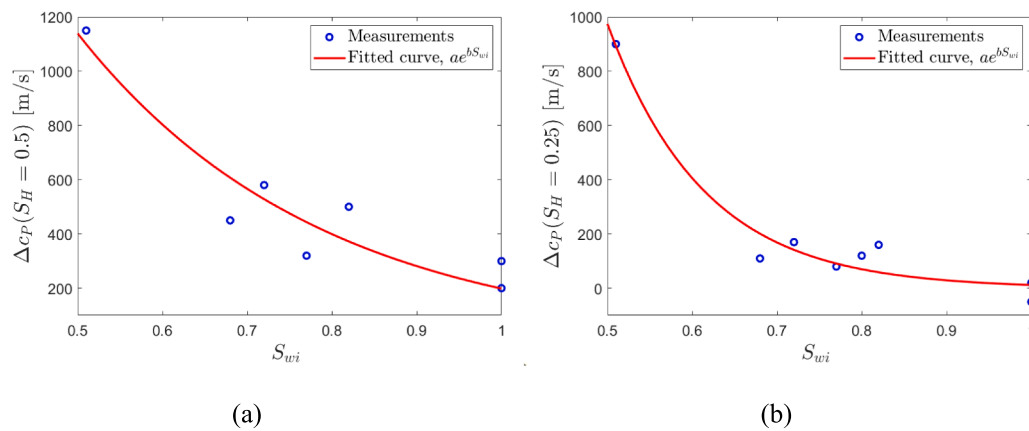
The sensitivity analysis detailed in section 2.4 indicates an uncertainty in  $c_p$  of 45 m/s for the results reported in Fig. 6. The change in  $c_p$  during hydrate growth, i.e. relative to the baseline velocity is set to 15 m/s.

### 3.5. Change in $c_p$ as a function of $S_{wi}$

In Fig. 7, the change in  $c_p$  (relative to the baseline velocity) as a function of  $S_{wi}$  is presented for all experiments at a fixed hydrate saturation, in (a)  $S_H = 0.5$  and (b) at  $S_H = 0.25$ . Fitting curves are also indicated in the figure. In (a), the data from experiment 5 ( $S_{wi} = 0.8$ ) is missing due to a logging computer crash. The y-axis is labeled  $\Delta c_p$ , i.e. the change in  $c_p$  relative to the baseline velocity for each of the experiments. It is evident that in the experiments where  $S_{wi}$  is lowest, the increase in  $c_p$  is highest. In experiment 1, where  $S_{wi} = 0.51$ ,  $\Delta c_p$  is 1150 and 900 m/s at  $S_H = 0.5$ , and 0.25, respectively. At  $S_H = 0.5$ , for the experiments having  $S_{wi}$  in the range 0.68–0.82,  $\Delta c_p$  is in the range 300–600 m/s. For the same experiments, at  $S_H = 0.25$ ,  $\Delta c_p$  is in the range 90–190 m/s. For experiments 7 and 8, where  $S_{wi} = 1$ ,  $\Delta c_p$  is 200 and 300 m/s, respectively at  $S_H = 0.5$ . For these experiments, at  $S_H = 0.25$ ,  $\Delta c_p$  is 20 and –50 m/s, respectively. The negative  $\Delta c_p$  comes from the decrease in the measured  $c_p$  reported in Fig. 6.

The sensitivity analysis detailed in section 2.4 indicates an uncertainty in the change in  $c_p$  of 15 m/s for the measurements presented in Fig. 7.

To highlight the decreasing tendency of  $\Delta c_p$ , fitting curves are included in Fig. 7. An exponential decreasing curve on the form  $ae^{bS_{wi}}$  is found to give the best fit. In Fig. 7(a) the coefficients  $a$  and  $b$  describing the fitting curve are 6534 and –3.494, respectively, with an r-squared ( $R^2$ ) value of 0.8791. In Fig. 7(b) the coefficients  $a$  and  $b$  describing the fitting curve are 78,130 and –8.768, respectively, with an  $R^2$  value of 0.9579. The fitting curves are obtained with the function fit() in MATLAB version 2021a. The  $R^2$  values are rather high, however, more



**Fig. 7.** The change in  $c_p$  (relative to the baseline velocity),  $\Delta c_p$ , as a function of  $S_{wi}$  is presented for all experiments at a fixed hydrate saturation. Fitting curves on the form  $ae^{bS_{wi}}$  are indicated. (a)  $\Delta c_p$  at  $S_H = 0.5$  with fitting curve coefficients  $a = 6534$  and  $b = -3.494$ , and (b)  $\Delta c_p$  at  $S_H = 0.25$  with fitting curve coefficients  $a = 78130$  and  $b = -8.768$ .

datapoints are needed to establish if such an exponential model is a good prediction of measurements reported on the form as shown in Fig. 7.

#### 4. Discussion

For consolidated sediments, an increase in  $c_p$  during hydrate growth in the laboratory has been generally explained with hydrates taking part and stiffening the solid frame, whereas hydrates are assumed to be forming within the pore fluid if little or no change in  $c_p$  is observed [7,12,23]. The same overall relation between hydrate formation pattern and  $c_p$  is reported for unconsolidated hydrate bearing sediments [4–6,11,13].

In general, the DEM predicts a drastic increase in  $c_p$  of a porous material if the low aspect ratio pores are filled with a solid material such as hydrate [21]. By filling the higher aspect ratio pores, the DEM predicts a modest increase in  $c_p$ . Little or no change in  $c_p$  is predicted by the Gassmann's equation by letting hydrate act as a fluid.

As hydrates forming in the pore fluid is considered to have little effect on  $c_p$ , the increase in  $c_p$  observed in experiment 1 ( $S_{wi} = 0.51$  in Fig. 4) is assumed to be caused by hydrates taking part in the solid frame. The measurements and calculations of the baseline velocity in Fig. 3, indicates that there is a uniform water/gas distribution for experiment 1. For such a distribution gas is at least partially available for lower aspect ratio pores and a portion of the hydrates will grow in these. Due to hydrophilic nature of sandstones, water will coat the pore walls for low  $S_{wi}$ . The hydrates will thus take part in the frame on the pore walls and not turn to a slurry mix of water and hydrate. This may explain the relatively rapid increase in  $c_p$  seen in experiment 1.

The results in experiments 2–8 are very different from experiment 1 in the sense that there is little change in  $c_p$  early in the hydrate formation process (Figs. 5–7). In Fig. 7 (b), this is clearly illustrated by the small change in  $c_p$  for  $S_H$  less than 0.25 for  $S_{wi} \geq 0.68$ . In (b),  $c_p$  tends to change less in the experiments with higher  $S_{wi}$ , indicating that hydrates form in the pore fluid when  $S_w$  is high. It has been argued that hydrate formation goes through two stages in water saturated pores; first a hydrate-water slurry stage and then a solidification stage [7]. This fits well with the results from experiments 2–8; After some initial stage of little change,  $c_p$  increase after a certain  $S_H$  in experiments 2–8. For higher  $S_{wi}$ , the water-hydrate slurry stage persists for a higher  $S_H$  compared with experiments with lower  $S_{wi}$ . More experiments could have been conducted in the  $S_{wi}$  range 0.51 – 0.68 to better describe the relation between cementing effects and hydrate formation. Such measurements could also add confidence in the tendency indicated by the fitting curves in Fig. 7.

In experiment 1, it was argued that some of the low aspect ratio pores were filled with hydrates from the very start of the hydrate formation process, leading to a clear increase in  $c_p$ . This can not be the case for

experiments 2–8. Due to the capillary effect and the hydrophilic nature of sandstones drawing water into small pore spaces, it may seem viable that small aspect-ratio pores are fully water saturated. Thus, in experiments 2–6, hydrates may form at the water–gas interface in the larger pores with higher aspect ratios, giving a more modest increase in  $c_p$ .

Some unexpected results are observed in Figs. 5–6. There is a small decrease in  $c_p$  for low  $S_H$  in experiments 2–8. In experiment 7 in Fig. 6 there is also a short increase prior to this decrease for  $S_H$  approximately 0–0.025. Seemingly similar findings have been reported for shear wave measurements by Hu et al. [7], where a decrease of approximately 60 m/s in the shear wave velocity ( $c_s$ ) was reported for  $S_H$  in the range 0 – 0.15. Such changes in  $c_p$  or  $c_s$  are not predicted by models for hydrates forming in the pore fluid. No explanation is provided in the current work for this change in  $c_p$ . It might be that free gas redistributes during the dynamic process of hydrate formation. Going from a patchy to a uniform or from a uniform to a patchy water/gas distribution (Fig. 3), may give a noticeable effect on  $c_p$ . Another potential explanation is that the volume expansion due to water forming into hydrate might cause small cracks in the sandstone, potentially softening the solid frame.

For an artificial consolidated porous ceramic material having  $S_{wi} = 1.0$ , hydrates were reported to form in the pore fluid for  $S_H$  less than 0.3 and form as part of the solid frame for  $S_H > 0.3$  [7]. These findings are similar to the findings in the present work. Hydrates have been reported in general to act as cement in “gas-rich” systems where the gas is interconnected through the sample (low  $S_{wi}$ ) [4] and hydrates grow at grain contact points. This trend is observed for experiment 1 ( $S_{wi} = 0.51$ ), where hydrates seem to take part in the solid frame early in the hydrate formation process.

#### 5. Conclusions

Measurements of the compressional wave phase velocity ( $c_p$ ) are presented as a function of hydrate saturation,  $S_H$ , during hydrate growth for Bentheim sandstone. Eight experiments were conducted on eight sandstone samples, having initial water saturation,  $S_{wi}$ , in the range 0.51 – 1. It is discussed how  $S_{wi}$  relates to whether hydrates take part in the solid frame or form in the pore fluid during hydrate growth.

In the measurements,  $S_{wi}$  and  $S_H$  are observed to have a clear impact on the measured  $c_p$ . Early in the hydrate formation process in experiment 1, which has the lowest  $S_{wi} = 0.51$ , a clear increase in  $c_p$  as a function of  $S_H$  is observed. The differential effective medium theory, ascribe such an increase in  $c_p$  to cementing effects in the soft, low aspect-ratio pores. This cementing effect is assumed to be due to high gas availability when  $S_{wi}$  is low. In the other experiments 2–8, where  $S_{wi} \geq 0.68$ , there is a hydrate formation stage for low  $S_H$  where little or no change is observed in  $c_p$ . This is ascribed to hydrates forming in the pore

fluid by e.g. Gassmann's equation. For higher  $S_H$  a second hydrate formation stage follows where  $c_p$  increase for increasing  $S_H$ . Such a stage has been referred to by others as a "solidification stage" where hydrates residing in the pore fluid eventually start bridging the pores, increasing the stiffness of the rock. From the measurements reported in the current work, the  $S_H$  interval defining the first hydrate formation stage increase for increasing  $S_{wi}$ .

In previous studies on both consolidated and unconsolidated hydrate bearing sediments, hydrates have been reported to act as cement in "gas-rich" (low  $S_{wi}$ ) systems and to form in the pore fluid in "water-rich" systems (high  $S_{wi}$ ). This description of the hydrate morphology fits well with the results obtained in the current study, where  $c_p$  is studied for hydrate-bearing sandstone.

### Declaration of Competing Interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

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### Data availability

The measurement data used in the current study is published with open access at UiB Open Research Data, DataverseNO, <https://doi.org/10.18710/GDT85X> [41].

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