Evaluating effort regulation in mixed fisheries: a 1 Monte Carlo approach 2 Xiaozi Liu^{1,2,3} and Mikko Heino^{*4,5,6} 3 ¹Institute of Economics, Academia Sinica, Taiwan 4 ²Future Oceans Lab, University of Vigo, Spain 5 ³Present address: NORCE Norwegian Research Center, Bergen, Norway 6 ⁴Department of Biological Sciences, University of Bergen, Norway 7 ⁵Institute of Marine Research, Bergen, Norway 8 ⁶International Institute for Applied Systems Analysis (IIASA), Laxenburg, Austria 10 2019 11 !!!Warning!!!

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Abstract

This paper evaluates whether effort regulation could achieve the goal of pro-13 tecting low-abundance species in mixed fisheries. We construct a two-species 14 bio-economic model and compare the stock abundance ratio in the end of the 15 fishing season with the ratio prior to the fishing. Fishers' profit maximization 16 problem is governed by three key factors: (a) the overall efficiency of catching 17 different species (catchability), (b) the price of different species, and (c) their 18 ability to catch the favoured species separately from the less-favoured species 19 (separability). Using a Monte Carlo sampling of feasible parameters space, we 20 show that effort regulation has good chances (87% of the cases) of maintaining 21 the end stock ratio near equal levels ($\frac{1}{2}$ < stock ratio < 2) when the initial stock 22 ratio is equal. If the initial stock ratio is not equal, however, there is a high risk 23 (about 50% of the cases) that effort control increases differences in the rel-24 ative species abundances, rather than diminishing them. The effects depend 25 on whether the key factors determining fishing profitability are counteracting 26 or reinforcing each other, and their relative strength. Our results warn against 27 placing too much faith on the ability of effort regulation to protect species at 28 low abundances from excessive exploitation. 29

30 KEYWORDS: mixed fisheries, effort control, bioeconomics modeling, Monte

³¹ Carlo approach, fisheries management

³² JEL CODES: Q22, Q57

33 1 Introduction

Total allowable catch (TAC) regulation, a form of output control, is a single-species management approach that sets stock-specific catch quotas (Stefansson and Rosenberg, 2005). In a mixed fishery where many species are caught simultaneously, management relying on stock-specific TACs can be impractical because of data requirements and costs, and be-

cause of discarding of over-quota catches (Daan, 1997; Hilborn et al., 2004; Baudron et al., 38 2010), or when discarding is not allowed, because species with restrictive quotas ('choke 39 species') prevent full utilization of species with more permissive quotas (Kuriyama et al., 40 2016; Alzorriz et al., 2018; Mortensen et al., 2018). To address these problems, input con-41 trol regimes, which are often species-unspecific and account for the multitude of species 42 living in an ecosystem, are sometimes favoured for the management of mixed fisheries 43 (Pope, 2002; Squires et al., 2017). Input control regimes set quotas at the operational unit 44 level; for example, quotas are given as total allowable fishing days per fleet category, fur-45 ther split among the individual license holders (Laurec et al., 1991; Andersen et al., 2010; 46 Danielsen and Agnarsson, 2018). 47

Effort regulation has been practised in many fisheries (Squires et al., 2017), including 48 some Mediterranean fisheries (Vielmini et al., 2017; Mulazzani et al., 2018), the sole and 49 plaice fisheries in the North Sea (European Union Committee, 2008), and the demersal 50 fisheries in Faroese waters (Jákupsstovu et al., 2007; Danielsen and Agnarsson, 2018). 51 Moreover, license control, a dominant fisheries management strategy in the Global South, 52 represents a special form of effort regulation. In these fisheries, a total number of licenses 53 is specified, often in combination with other measures such as seasonal fishing bans (FAO, 54 2009; Shen and Heino, 2014; Tromeur and Doyen, 2018). 55

The fishing days system in the Faroe Islands is one of the most studied examples of 56 effort regulation (Jákupsstovu et al., 2007; Baudron et al., 2010; Danielsen and Agnarsson, 57 2018). The system was introduced in 1996 to manage the demersal fisheries with cod, 58 haddock and saithe as their main targets. While sometimes hailed as highly successful, a 59 10-years appraisal study by Jákupsstovu et al. (2007) showed that Faroese Total Allowable 60 Effort (TAE) system did not achieve some of its key objectives, namely controlling the 61 fishing mortality of the key species. This conclusion has been upheld by later assessments 62 (Danielsen and Agnarsson, 2018). Most fishers opportunistically targeted the most valu-63 able species, cod, leading to high levels of mortality for this valuable stock even when less 64 abundant. The design of TAE system in the Faroe Islands relied on the assumption that 65

when fishers choose their target species to maximize their profit, they target the species that provide the highest catch rates and 'automatically' protect the less abundant species with lower catch rates (Jákupsstovu et al., 2007; Baudron et al., 2010; Danielsen and Agnarsson, 2018). However, this is an assumption rather than a fundamental property of effort-controlled fisheries.

Previous studies on TAE regulation have often been conducted in a single species set-71 ting and in comparison with TACs; for example, fishing vessel behaviour under TAE and 72 TAC regulation (Anderson, 1999; Stefansson and Rosenberg, 2005), and the effect of un-73 certainty on the efficiency of catch or effort controls (Danielsson, 2002; Yamazaki et al., 74 2009). Another strand of literature examined the degree of input substitution between re-75 stricted inputs and unrestricted inputs in a TAE system. Examples include the substitution 76 intensity of restrictions on fishing days versus restrictions on vessel tonnage of the British 77 Columbia commercial salmon fishery (Dupont, 1991), and the substitution between physi-78 cal inputs and fishing location of the UK beam trawl fishery (Pascoe and Robinson, 1998). 79 Until now, effort regulation has been assessed in a context of specific fishery systems. How-80 ever, case-specific detail may hinder identifying the key factors that determine the success 81 (or failure) of effort regulation in mixed fisheries. 82

The key factors affecting fishers' targeting decision in mixed-fisheries have previously 83 been studied piece by piece; for example, Katsukawa and Matsuda (2003) focused on the 84 effect of non-linear catchability, Noailly et al. (2003) on the effect of price on switching 85 harvest strategies, and Tromeur and Doyen (2018) on the effect of technical interactions. 86 As a result, the conclusions of these papers may differ depending on specific underlying as-87 sumptions. When perfect separability is assumed, target switching may be able to protect 88 the less abundant species from being overfished (Katsukawa and Matsuda, 2003; Bischi 89 et al., 2013a,b); when joint production is unavoidable, species with lower price and growth 90 but higher intraspecific competition and catchability are more prone to overfish, as con-91 cluded by Tromeur and Doyen (2018). We attempt to study all these key aspects together 92 to give a more holistic picture about their interplay. We are specifically interested in effort 93

regulation of mixed fisheries, but our results can be interpreted more generally as representing profit-oriented, effort-limited exploitation that could occur in unregulated fisheries
or in a single-owner case.

The purpose of this paper is to present a generic analysis of factors determining the 97 practicality of effort regulation using a simplified two-species fishery system. We gener-98 alize earlier models by treating separability and stock elasticity of harvest as parameters; 99 the former describes fishers' ability to target and catch a specific species and the latter the 100 degree of schooling behaviour of the fish. Our aim is to show when the effort regulation 101 approach can work in terms of achieving the biological goal of not exhausting any of the 102 species, or when it may not work, and why. The rest of the paper is organized as fol-103 lows. The first section illustrates key factors governing fisherman's targeting decision and 104 detailed model specifications. In the subsequent sections, we first present an analytical opti-105 mal harvest rule based on a common assumption about catchability parameter, followed by 106 an evaluation of effort regulation based on a generic set-up using Monte Carlo simulations. 107

108 2 Methods

Identifying key factors

We start by identifying three key factors that describe the dynamics of a mixed fishery: the relative abundance and catchability of fish stocks, which determine the potential catch rates; the relative price for different fish species, which relates to the revenues obtained; and the ability of fishermen to catch the favoured species separately from the unfavoured species. These three factors form the cornerstones of effort regulation (Fig. 1).

Catchability is a species-specific parameter that describes the efficiency of fishing operation in catching a certain type of fish, therefore depending on both characteristics of the target (e.g., fish behaviour) and the fishing operation (e.g., efficiency of the fishing gears). Typically, catchability q of species i is defined through a linear relationship between catch rate (C_i), effort (E), and stock abundance (N_i), $C_i = q_i E N_i$. However, this simple model is



Figure 1: Key factors determining the practicality of effort regulation

often acknowledged to be inappropriate (Winters and Wheeler, 1985; Hilborn and Walters, 1992; Harley et al., 2001); for instance, a high catch per unit effort (C/E) for schooling species can still be maintained even at a low level of stock abundance. We thus follow the alternative formulation proposed by Steinshamn (2011) and Liu and Heino (2013) where catchability is measured in terms of the local stock density ρ experienced by a fisher:

$$C_i = q_i E \rho_i = \tilde{q}_i E N_i^{b_i} = a_i q_i N_i^{b_i - 1} E N_i, \text{ with } \rho_i = a_i N_i^{b_i}.$$
(1)

Thus \tilde{q}_i in Eq. 1, termed local catchability, is analogous with q_i in the classic formulation, but it has absorbed the scaling parameter a_i and is measured relative to local density ρ_i . N_i is stock abundance normalized against carrying capacity K_i . Parameter b_i is stock elasticity of harvest, with a typical value between $0 \le b_i \le 1$. The limit case ($b_i = 0$) refers the species that is extremely schooling and the fishers can locate the schools perfectly. $b_i = 1$ represents a non-schooling species that is uniformly distributed.

The influence of the market is captured by the relative price of the two species. We consider two ways of price determination: i) exogenous price, in which price is constant,

and ii) endogenous price, in which price is a decreasing function of the catch. Specifically,

$$p_i(C_i) = \max\left(0, p_{i,0}\left(1 - \omega_i(C_i - C_{i,0})\right)\right),\tag{2}$$

where $p_{i,0}$ is the initial unit price and $p_{i,0}\omega_i$ is the slope of the price function. When $\omega_i = 0$, $p_{i,0} = p_{i,0}$ and the price is constant (exogenous price); when $\omega > 0$, price is endogenous, with higher total catches resulting in reduced unit price. The price $p_{i,0}$ is obtained when $C_i = C_{i,0}$, where $C_{i,0}$ is the optimal catch on the first fishing day when $\omega_i = 0$. That is to say, we express the price relative to the price obtained during the first fishing trip.

The final element in our model is 'separability' (τ). This is a fishery-level parameter 126 and refers to fishers' ability to catch the favoured species, or in economics jargon, to the 127 degree of joint production. It depends on biological factors (e.g., intrinsic differences in 128 behaviour and micro-habitat use of the alternative species), fishers' skill of using these 129 differences in fishing, and available fishing technologies that fishers can utilize (Branch 130 and Hilborn, 2008; Squires et al., 2017). We take $\tau = 1$ to mean perfect separability where 131 only the targeted species is caught, and $\tau = 0$ complete inability to catch species separately 132 such that the total effort is equally shared among the two harvested species. For every unit 133 of fishing effort made by a fisherman (e_i) , only fraction $\frac{1+\tau}{2}$ is effectively converted into 134 catching the target species (i), whereas fraction $\frac{1-\tau}{2}$ 'leaks' to the other species, leading 135 to its bycatch. Thus, we differentiate the nominal effort targeted on species i, e_i , and the 136 effective effort E_i , where $E_i = \frac{1+\tau}{2}e_i + \frac{1-\tau}{2}e_{-i}$ and e_{-i} denotes effort targeting the other 137 species. 138

¹³⁹ Biological model and assessment criteria

We model a simple fishery system consisting of two species that share the same overall habitat but are otherwise independent. Discarding is assumed not to occur. Our model focuses on stock dynamics in a single fishing season, which comprises a number of fishing trips of equal length; the length is inconsequential for our analysis and we will assume daily trips for convenience. Recruitment is assumed to occur outside the fishing season and
can thus be ignored.

If stock abundance in the beginning of a fishing day/trip is N_0 , it will drop to N_t in the end of that fishing trip due to natural and fishing mortality. The stock dynamics ¹ is specified in the following:

$$N_{t} = \begin{cases} N_{0}e^{-(F_{t}+M)} = N_{0}e^{-(\tilde{q}E_{t}+M)t} & \text{if } b = 1, \\ \left\{ \left[N_{0}^{1-b} + \frac{\tilde{q}E_{t}}{M} \right]e^{-M(1-b)t} - \frac{\tilde{q}E_{t}}{M} \right\}^{\frac{1}{1-b}} & \text{if } 0 \le b < 1. \end{cases}$$
(3)

where F and M are respectively fishing and natural mortality. Other notations follow Eq. 1. 149 The key question is whether profit-oriented fishing can lead to protection of the less 150 abundant species? We use the stock size ratio as the metric to assess this question. As long 151 as natural mortality during the fishing season is negligible, changes in this metric are driven 152 by harvesting. If the stock ratio in the end of the fishing season $r_T = N_1^T / N_2^T$ is closer to 153 unity than the initial stock ratio $r_0 = N_1^0/N_2^0$, then the originally less abundant species must 154 have suffered less from fishing than the other species. In other words, it has been offered a 155 degree of protection. This is a necessary condition for effort regulation to have the potential 156 to be successful. We emphasize, however, that this criterion is not a sufficient condition to 157 ensure sustainable fisheries, because it does not address simultaneous stock depletion. This 158 could be prevented by setting the total effort quota sufficiently low; the determination of 159 suitable total effort is beyond the scope of our current analysis. 160

We consider two basic scenarios in our analysis: (a) 'even' scenario in which two species in the mixed fishery have the same initial stock (i.e., $r_0 = N_1^0/N_2^0 = 1$); (b) 'biased' scenario in which their initial stock levels are different (here $r_0 = 2$). In the former case, the success criterion is that the final stock size ratio r_T does not deviate too much from unity, and in the latter case, that the final stock size ratio r_T has moved closer to unity.

¹The expression for N_t is derived via integrating over a full fishing trip $\frac{dN}{dt} = -(F+M)N$, and $F = \tilde{q}N^{b-1}E$. For detailed derivation see Steinshamn (2011); Liu and Heino (2013)

¹⁶⁶ **Profit maximizing fleet**

The goal of the fleet manager is to maximize her payoffs per fishing trip for the entire fleet. We define effort in terms of fishing days. The total allowable fishing days per fishing season allocated to a fleet is set at Q. We assume the fleet consists of n identical boats. The strategy option for the manager is to decide the number of boats to target different species $i \in (1,2)$. The maximization will be repeated for each fishing trip until Q is exhausted or profit turns negative. We formulate trip-level profit maximization as follows:

$$V_{t} = \max_{e_{i,t}} \sum_{n} \sum_{i} \left(\int_{0}^{C(E_{i,t})} p_{i}(C) dC - ce_{i,t} \right), i \in (1, 2)$$

$$\sum_{i} e_{i,t} \leq n \ (Fleet \ capacity)$$

$$s.t. \sum_{t} \sum_{i} e_{i,t} \leq Q \ (Effort \ control)$$

$$E_{i,t} = \frac{1+\tau}{2} e_{i,t} + \frac{1-\tau}{2} e_{-i,t} \ (Separability)$$

$$V_{t} \geq 0 \ (Non-negativity)$$

$$(4)$$

where price of fish p_i is determined by the price function in the Eq. 2; *c* is cost per unit effort, *e* and *E* denote respectively nominal effort and effective effort. Provided that the species are not fully separable, Eq. 4 gives two sources of income streams from each species. *C* denotes total catch per trip, given by the function by Liu and Heino (2013), based on the catchability definition in Eq. 1:

$$C_{t} = \tilde{q}E_{t} \int_{0}^{1} N_{t}^{b} dt$$

$$= \begin{cases} \frac{F_{t}}{F_{t}+M} N_{0}(1-e^{-(F_{t}+M)}) = \frac{\tilde{q}E_{t}}{\tilde{q}E_{t}+M} N_{0}(1-e^{-(\tilde{q}E_{t}+M)t}) & \text{if } b = 1, \\ \tilde{q}E_{t} \int_{0}^{1} \left\{ \left[N_{0}^{1-b} + \frac{\tilde{q}E_{t}}{M} \right] e^{-M(1-b)t} - \frac{\tilde{q}E_{t}}{M} \right\}^{\frac{b}{1-b}} dt & \text{if } 0 \le b < 1. \end{cases}$$
(5)

The maximization problem in Eq. 4 is subject to several constraints: (1) fleet capacity constraint: total fishing boats per trip shall not exceed the fleet capacity n, assuming trip length of 1 day/trip; (2) effort constraint: total fishing days per season is no more than Q; (3) species separability constraint: only part of the effort is converted into effective effort; and (4) non-negative profit per fishing trip.

Because more boats targeting the same species result in faster depletion of the resource, 183 and may influence the price (if $\omega > 0$), the optimal decision of one fisherman depends on 184 what other fishermen decide to do. This can potentially lead to a game-like situation, but 185 this is avoided if we assume that the decision horizon is one fishing trip (e.g., 1 day) only, 186 and the problem reduces to a simple optimization task analogous to 'perfect competition' 187 of identical competitors in economics, or 'ideal free distribution' in ecology (Fretwell and 188 Lucas, 1969). Thus, to understand the collective behaviour of individual fishermen, we can 189 simply find the distribution of effort that maximizes the collective pay-off per fishing trip. 190 The solutions of the model correspond to optimal policies in a single owner case too. 191

¹⁹² Monte Carlo sampling method

The model is not analytically tractable except for some special cases. To obtain an overview 193 on how key factors affect the performance of effort regulation, we turn to the Monte Carlo 194 method of repeated random sampling approach. Key factors and their assumptions are sum-195 marized in Table 1 and are very general. We assume b and τ to follow uniform distribution 196 because they are naturally bounded between 0 and 1 (while b could exceed 1, b = 1 is a 197 defensible upper limit, see Steinshamn (2011)). Price and catchability ratios are assumed 198 to be log-normally distributed such that the mean ratio is one. The results are based on 199 50,000 random replicates. 200

3 Optimal harvest decisions in a mixed fishery

202 A static setting

For the case of uniformly distributed fish stock (b = 1), we can analytically show that optimal harvest decision in our model is characterized by the relative marginal profit of effort (MPE) of the two stocks, i.e., the difference in the marginal increase of profit when

Table 1: Key assumptions for Monte Carlo sampling. Actual levels of prices and costs are immaterial as long as fishing is profitable.

Parameter	Description	Value	Distribution
τ	separability	$0 \le \tau \le 1$	uniform
b	stock elasticity of harvest	$0 \le b \le 1$	uniform
$\log(\frac{p_1}{p_2})$	price ratio	$\mu=0, sd=0.5$	normal
$\log(\frac{\tilde{q}_1}{\tilde{q}_2})$	catchability ratio	$\mu=0, sd=0.5$	normal
ω_i	slope of the price function	0 or 50	n.a.
M_i	natural mortality	$0.2 { m yr}^{-1}$	n.a.
Q	effort quota	1000 days	n.a.
n	fleet capacity	20	n.a.

Note: μ denotes mean and *sd* standard deviation.

²⁰⁶ effort targeting a specific species is increased. We can distinguish three cases:

• If MPE₁ >MPE₂, then only species 1 is harvested ($e_1 > 0$ and $e_2 = 0$).

• If MPE₁ <MPE₂, then only species 2 is harvested ($e_1 = 0$ and $e_2 > 0$).

• If MPE₁ =MPE₂, then both species are harvested ($e_1 > 0$ and $e_2 > 0$).

The expression for MPE in the general case is too complicated to yield insight (see the Appendix). However, if we assume that natural mortality is insignificant over short time periods and can be ignored (M = 0), MPE₁ >MPE₂ if $p_1\tilde{q}_1N_1e^{-\tilde{q}_1E_1} > p_2\tilde{q}_2N_2e^{-\tilde{q}_2E_2}$. High price p and initial stock N will therefore favour targeting one stock over the other. The role of catchability \tilde{q} is ambiguous because its effect can be either positive or negative, depending on the other parameters.

²¹⁶ When fishers cannot discriminate the two species ($\tau = 0$), every unit of effort is equally ²¹⁷ divided between them, and any effort allocation satisfying the fleet capacity constraint will ²¹⁸ be optimal. This is a trivial case, and in the subsequent discussion we will focus on the ²¹⁹ case $\tau > 0$ only.

220 Seasonal patterns of harvest decisions

Because a fishing season consists of a number of fishing trips in our model, we will study how MPE evolves over time. There are three generic patterns of time evolution in the model:

- A single species is the sole target species during the whole fishing season. MPE of one species is always greater than the other.
- A single species is the sole target species in the beginning of the fishing season. After MPEs are equalized between the species, both species are targeted.
- A single species is the sole target species in the beginning of the fishing season.
 MPEs switch the rank that leads to a target switch, i.e., the other species becomes the sole target.

The first two cases follow naturally from the rules of optimal harvest described in the 231 previous section: the fishermen will target the more profitable stock, or if both stocks are 232 equally profitable, they will split their effort such that the equal profitability is maintained. 233 Initially, one stock is almost always more profitable. Whether targeting the more profitable 234 species leads to equal profitability during the period of interest depends on the details. First, 235 while targeting one species will often cause the MPEs to converge towards each other, this 236 is not always the case. MPEs may diverge if separability τ is low, or if one species has 237 higher natural mortality M than the other. Second, even when targeting one species is 238 causing the MPEs to converge, full equalization might not be reached during the available 239 fishing season. 240

Fig. 2a–c illustrates how targeting one species reduces its profitability, eventually resulting in the situation in which both species have similar MPEs. In this example, species 1 has initially a higher MPE and is the sole target during the first part of the season. Over time, MPE for the target species 1 decreases more than MPE for the bycatch species 2 because fishing reduces its abundance more than that of the bycatch species. When both species reach the same MPE level, the effort (Fig. 2b) is divided between the two species such that the MPE equality is maintained. In this example, effort regulation first causes divergence in the relative stock abundances, followed by rebalancing and divergence to the other direction.



Figure 2: Two qualitatively different scenarios of marginal profit of effort and effort allocation over time, together with the corresponding relative stock size. On the top row (a–c), separability is high ($\tau = 0.8$). Two distinct phases are observed: first, only the species 1 that is more profitable is targeted, and second, once the profitability of species 1 is reduced to that of species 2, both species are targeted with an effort allocation that keeps their profitability similar. On the bottom row (d–f), separability is lower ($\tau = 0.57$). This leads to dynamics that are initially similar, but instead of profitability equalization, the initial bycatch species becomes the sole target. Parameters other than τ are equal for both scenarios: $N_0 = [0.5, 0.5]$, b = [0.813, 0.086], p = [53924, 100000], $\tilde{q} = [0.0003, 0.0003]$, $\omega = [0,0]$, c = 0.1, Q = 1000.

The dynamic in the third case where the MPE curves of two species cross each other and the fishermen switch their target species is more intricate. Fig. 2d–f illustrates how such target switching can result from effort 'spill-over'. Fishermen first target the more profitable species 1. As its profitability declines, both species 1 and 2 become targeted. At this point, it is possible that even when species 2 is the sole target, species 1 is caught so much as bycatch that its MPE stays lower than that of the target species. We will elaborate
 further on this point in the Section 4 when discussing reinforcing effect.

4 Assessing performance of effort regulation through Monte Carlo simulations

259 The overall performance of effort regulation

We assess performance of effort regulation by simulating a large number (50,000) of cases 260 generated by sampling a realistic parameter space (Table 1). When the fisheries are initiated 261 with two species at equal abundance, effort regulation can often keep the relative stock 262 levels within 'reasonable' bounds. Specifically, if we require that the stock ratio N_1^T/N_2^T at 263 the end of fishing season remains within the interval [0.5, 2] (i.e., the less abundant species 264 has density at least 50% of that of the more abundant species), effort regulation is successful 265 in 87% of the cases (Fig. 3a). However, if the fisheries are initiated with one species 266 being twice as abundant as the other one, the chances of effort regulation meeting the 267 same success criterion are considerably lower, about 51% (Fig. 3b). In these cases, effort 268 regulation has either maintained the original biased stock ratio, or 'corrected' it towards 269 equality. However, there is also a sizeable proportion of cases -40% – where the relative 270 stock abundance becomes driven towards more extreme bias in favour of the originally 271 more abundant species. In the remaining fraction of the cases, the originally less abundant 272 species becomes more abundant as a result of fishing. 273

274 Single-factor effects

²⁷⁵ We now investigate the characteristics of the cases where effort regulation can be success-²⁷⁶ ful. Figures 4 and 5 show the density distributions of the final stock ratio against key ²⁷⁷ parameters that we varied. They reveal two main patterns. First, the fishers' ability to ²⁷⁸ catch target species, separability τ (the only stock-unspecific parameter we varied), has



Figure 3: Histogram of stock ratio in the end of the fishing season for (a) even $(N_1^0 = N_2^0)$ and (b) biased initial stock ratio $(N_1^0/N_2^0 = 2)$. Cyan bands indicate the range where end stock ratio is seen as 'reasonable', defined as $N_1^T/N_2^T \in [0.5, 2]$. Price is constant ($\omega = [0, 0]$); other parameters as detailed in Table 1.

an important role. When separability is low $(\tau \rightarrow 0)$, stock ratio at the end of the season 279 usually stays near its initial value, be it equal or biased (Fig. 4a and 5a). However, when 280 separability is high $(\tau \to 1)$, the stock ratio diverges away from its initial value, in one 281 direction or the other. If the initial stock abundances are even, then a bimodal distribution 282 emerges (Fig. 4a). If the initial relative stock abundances are biased, then the final stock 283 ratio shows a unimodal but skewed distribution (Fig. 5a). Across all τ , there is a tendency 284 for the stock ratio to move closer to unity; the average final stock ratio is $N_1^T/N_2^T 0 \approx 1.15$, 285 although there is a long tail of cases towards more extreme bias (Fig. 5a). Nevertheless, in 286 an average sense, effort regulation offers a degree of protection for the less abundant stock 287 when starting from unequal initial abundances. 288

Second, the parameters that are stock-specific show similar patterns. If the relative stock abundances are initially even, the abundances at the end of season have best chances of maintaining the status quo when the species are similar in terms of their schooling parameter *b*, catchability \tilde{q} , and price *p* (Fig. 4b–d). On the other hand, if the initial relative stock abundances are biased, then the similarity of the species, on average, tends to hinder equalization of relative abundances. However, if the species differences are such that the initially less abundant species is a more favourable target (higher price *p* or catchability \tilde{q} , or lower stock elasticity to harvest *b*), then equalization is more likely to happen (Fig. 5b– d). Differences in the opposite directions will consequently make equalization less likely.

Most Monte Carlo replicates in Figures 4 and 5 show targeting of the same species through the fishing season. This happens because MPEs of the two stock converge so slowly that they do not meet during the available time, or because of the bycatch effect that may even make them diverge. Equalization of MPEs followed by targeting of both species for the rest of the season (similar to Fig. 2a–c) happens only in about 15% of replicates. Target swapping (Fig. 2d–f) is even rarer, occurring in about 4% of replicates for the even initial scenario and less than 1% of replicates for the biased initial scenario.



Figure 4: Density plots for the 'even' scenario (initial stock ratio $N_1^0/N_2^0 = 1$): black curves are contour lines, blue curves indicate the smoothed median density, and black dotted lines are reference level when the two species are symmetric. Price is declining with increasing catches ($\omega = [50, 50]$); other parameters as detailed in Table 1.

305 Interaction effects

When the species differ in more than one parameter, these differences could either reinforce or compensate for each other. For example, if one species has a higher unit price but



Figure 5: Density plots for the 'biased' scenario (initial stock ratio $N_1^0/N_2^0 = 2$ indicated by red dotted lines): black curves are contour lines, blue curves indicate the smoothed median density, and black dotted lines are reference level when the two species are symmetric. Price is constant ($\omega = [0,0]$); other parameters as detailed in Table 1.

lower catchability, it can be an equally attractive target to a cheaper species with higher catchability. This 'compensation effect' is seen in Figure 6 as contour lines that are tilted relative to the axes. In particular, a balanced final stock ratio can be achieved not only when the two species are similar, but also when they differ such that an attractive attribute is compensated by a less attractive one.

Conversely, when the species differ in multiple ways that work in the same direction, we observe a 'reinforcing effect'. This corresponds to the movement perpendicularly to the contour lines in Figure 6. In this case, even relatively small differences in the speciesspecific parameters may lead to large differences in the final stock ratio.

317 **5 Discussion**

We have addressed two questions that are pertinent to any effort control system: whether species that are originally balanced (i.e., similar in stock size) can be maintained at a relatively balanced level as a result of profit-oriented fishing, and secondly, whether profitoriented fishing could conserve species that are at low levels, such that relative stock levels



Figure 6: Parameter interactions under the even initial stock scenario for ratio of catchabilities (\tilde{q}) versus difference in the stock elasticity of (a) harvest (schooling, b) and (b) ratio of prices (p). Colour gradient shows the end stock ratio $\log_2(N_1^T/N_2^T)$. High stock differences are found when the effects of two factors are reinforcing each other. Similar stock levels appear around the mid-range area shown in white.Price is constant ($\omega = [0,0]$); other parameters as detailed in Table 1.

would be more balanced after the fishing season—a necessary, but not sufficient, condition 322 for a sustainable use of an ecosystem. We have addressed these questions using a generic 323 two-species dynamic bio-economic model, assuming fishers that are omniscient and profit-324 maximizing. Our main finding is that effort regulation is prone to exaggerating the stock 325 abundance differences, particularly when the fishers are effective in selectively catching the 326 more profitable species. Generally speaking, it is hard to achieve balanced relative stock 327 levels. However, effort regulation may achieve its biological conservation goal under two 328 general conditions: 329

- The species are sufficiently similar with respect to the key factors that determine the
 profitability of their harvest.
- 332 2. WI
- 2. When the key parameters counteract each other such that the resulting overall profitability is similar.

Concerning the latter case, a low catchability can be compensated by a higher price, and vice versa. On the contrary, if the key parameters reinforce each other, instead of counteracting, effort regulation can lead to increased differences in the relative stock levels, e.g. fishers keep harvesting the less abundant species. The degree to which one stock gets depleted depends on the fleet's capacity to deplete the stock (the total allowable effort Q and catchability \tilde{q}) as well as on the degree to which high local density is maintained when stock is being depleted (stock elasticity of harvest *b*).

Empirical studies have established that fishers' behavioural choices can, to a large part, 341 be understood based on their expectations on profits. Much of the evidence comes from 342 studies on location choice (e.g., Eales and Wilen, 1986; Gillis et al., 1993; Andersen et al., 343 2010). Our model predicts that in the beginning of a fishing season, profit-maximizing 344 fishers often target only a single stock. As that stock is fished down, its profitability declines 345 and eventually equals that of the other stock. At this point, fishers would be expected to 346 split their effort targeting both stocks. This kind of dynamic has been reported from the 347 Turks and Caicos Islands, where the artisanal fishermen diversified their effort allocation 348 after density of the initially favoured, more valuable target had sufficiently declined; price 349 difference between the two targets was constant and did not influence targeting (Béné and 350 Tewfik, 2001). 351

Because profitability reflects a range of biological and economic parameters, target 352 switches can occur in response to various factors, singly or together. For example, in 353 demersal fisheries of Northeast Atlantic, changes in catchability caused by technological 354 change are an important factor explaining long-term changes in target species (Marchal 355 et al., 2006). In a mixed coastal trawl fishery in Taiwan, the fishers responded to day-to-356 day price fluctuations by increasing catches of species with positive price signals (Liu et al., 357 2018). The failure of the Faroese fisheries to switch away from catching depleted species 358 was likely caused by price compensation (Jákupsstovu et al., 2007). Studies of small-scale 359 fishermen have shown simultaneous influences of seasonal fluctuations in catchability and 360 changes in price that lead to target switching (Salas et al., 2004; Naranjo-Madrigal and 361 Bystrom, 2019). 362

Our results show that differences in stock elasticity of harvest (*b*), reflecting a stock's spacing behaviour and the fishers' ability to find the fish, can be as important as differences

in the parameters traditionally emphasized when estimating revenues, namely catchability 365 and price (Fig. 4 and 5). While it is commonly acknowledged that the relationship be-366 tween fish abundance and catch may not be linear, theoretical analyses typically assume 367 that stock elasticity of harvest is unit-elastic (b = 1) or perfectly inelastic (b = 0); see Stein-368 shamn, 2011; Liu and Heino, 2013). Differences in b imply that the relative profitability 369 of two species might switch ranks even when they both see similar proportional reduction 370 in abundance. We are not, however, aware of any examples where changing in targeting 371 can be explained by differences in b. While empirical analyses will implicitly account for 372 this effect, it is probably difficult to detect in practice. Nevertheless, our results show that 373 effort regulation is likely to fail when a mixed fishery is composed of a schooling and a 374 non-schooling species. 375

Separability, or the ability of fishers to target and catch a species separately from oth-376 ers, has a multifaceted role in effort regulation of mixed fisheries. The fishers' ability to 377 target the more abundant species lies at the core of the idea that effort regulation can protect 378 species that are at low abundance. Our results show that separability is indeed necessary 379 for fishery to be able to selectively harvest the more abundant species (Fig. 5a). How-380 ever, strong separability also increases the risk of seriously depleting one of the species 381 (Figs. 4a and 5a), which can happen when one species has much higher price, catchability, 382 and/or schooling tendency than the other. When separability is poor, such extreme out-383 comes are mostly avoided, but poor separability also prevents fishers from fishing down 384 the more abundant species (Fig. 5a). The effect of separability is approximately linear, 385 such that studies assuming perfect separability (Katsukawa and Matsuda, 2003; Bischi 386 et al., 2013a,b) and complete lack of separability (Tromeur and Doyen, 2018) capture the 387 extremes-realistic situations likely lie somewhere in between. 388

It is worth noting that effort regulation incentivizes fishers to improve separability only when it helps them to increase the total value of their catches; there is no disincentive per se for catching non-target species. This is in stark contrast to catch quota regulation where lack of separability may prevent fisheries from fully utilizing quotas of some species (e.g., Kuriyama et al., 2016; Mortensen et al., 2018), hence incentivizing investments to
technology that improves separability. In any case, the degree to which fishers can adapt
their catch profiles is a core question for mixed-fisheries management (Hoff et al., 2010).

Our model includes only two species, while most fisheries are considerably more diverse. Our analysis indicates that profit-oriented exploitation can help to maintain a balance between two exploited species, but also that this requires a fortuitous balance between a number of biological and economic parameters. It is worth emphasizing that the higher is the number of exploitable species in a system, the more likely is that at least one of them does not meet this fortuitous balance. Therefore, challenges in using effort to regulation to manage mixed fisheries will increase with increasing species diversity.

In our analysis, we have solely focused on stock dynamics during a single fishing sea-403 son. Dynamics between fishing seasons could either exacerbate or alleviate the differences 404 in stock levels, depending on the processes related to biomass gain and loss (i.e., gain from 405 recruitment of new individuals and body growth of existing individuals, and loss through 406 mortality) that are stock-specific. Because of density-dependent effects, we can offer some 407 general insights. If a stock is below the stock level that corresponds to maximum biomass 408 production-and maximum sustainable yield (MSY)-then its biomass production will 409 usually increase with increasing stock size. This implies that the relatively more depleted 410 stock will also, on average, have lower biomass production, exacerbating the already ex-411 isting difference in the stock levels. On the other hand, if two stocks are larger than their 412 respective MSY levels, then the larger stock will see less growth, and the difference in the 413 stock levels is expected to decline. This suggests that effort regulation is more likely to 414 afford a degree of protection to less abundant stocks when most stocks are at healthy levels 415 (near MSY or higher), but that trusting effort regulation to conserve already depleted stocks 416 will be particularly pernicious. 417

Based on our numerical results and the arguments presented above, we suggest that effort regulation is most likely to succeed when (1) the fishery is catching only a few species, (2) these species are biologically similar and have similar market niches (such that the

parameters determining revenues are similar), and (3) the species are at 'healthy' abun-421 dance levels. The first two conditions are probably most likely to be fulfilled in cold-water 422 ecosystems where species diversity is low and taxonomically closely related species such 423 as gadids dominate catches. Conversely, effort regulation is likely to fail to protect at least 424 some species in species-rich temperate and tropical ecosystems—even more so when the 425 fisheries already are overexploited, such as in the Mediterranean Sea, where effort reg-426 ulation is a part of the management toolbox and the overall status of fisheries resources 427 remains poor (FAO, 2018). However, the fact that the effort control system for the Faroese 428 demersal fisheries came close to fulfilling the first two desiderata and yet failed suggests 429 that effort control lacks robustness even under relatively favourable conditions. 430

The fragility of effort regulation is further increased if markets are paying a price premium for rare species, as is the case for, e.g., Pacific bluefin tuna in Japan (Tokunaga, 2017). This effect could be countered by consumer awareness campaigns, which have been successful in the past in promoting more sustainable fishing practices (Jacquet et al., 2010).

Effort regulation is sometimes advocated as the solution to problems in managing mixed 435 fisheries that is simpler, more flexible, and easier to implement than species-specific TAC 436 regulation (Pope, 2002; European Commission, 2012). While some of these advantages are 437 undeniable, our results warn against placing too much confidence on the ability of effort 438 regulation to provide automatic protection for species that are depleted. Protection is only 439 expected to occur when the targeted species initially offer similar profitability. This re-440 quires a fortuitous balance between a range of biological and economic parameters, which 441 can be easily broken by exogenous or endogenous changes in prices. In this regards, sup-442 plementary regulations such as area management and gear restriction are needed, and a 443 combination of TAC and TAE is sometimes more favourable (Squires et al., 2017). 444

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576 Appendix: Derivation of the optimal harvest rules

⁵⁷⁷ We rely on the Lagrangian conditions to characterize the optimal harvest rules. The scope ⁵⁷⁸ of analysis in this section is limited to the case where the Baranov catch equation (also ⁵⁷⁹ known as Beverton–Holt model) applies (i.e., b = 1 in Eq. 5) and when the price is exoge-⁵⁸⁰ nous.

We formulate the Kuhn-Tucker (KT) Lagrangian function of Eq. 4, and derive following KT conditions:

$$\frac{\partial \bar{L}}{\partial e_i} = A_i \frac{1+\tau}{2} + A_{-i} \frac{1-\tau}{2} - c - \lambda \le 0$$
(6a)

$$e_i \frac{\partial L}{\partial e_i} = 0 \text{ and } \lambda(\sum_i e_i - n) = 0$$
 (6b)

$$\lambda \ge 0, e_i \ge 0 \text{ and } \sum_i e_i \le \min(n, Q - \sum_{t=1}^{t-1} e_{i,t})$$
(6c)

where $A_i = p_i q_i N_i \left(\frac{M}{(E_i q_i + M)^2} (1 - e^{-(q_i E_i + M)}) + \frac{E_i q_i}{E_i q_i + M} e^{-(q_i E_i + M)} \right)$. Note that $A_i \frac{1 + \tau}{2} + A_{-i} \frac{1 - \tau}{2} - c$ in Eq. 6a can be interpreted as marginal profit of effort (MPE). Analysis of Kuhn-Tucker conditions reveals a general optimal harvest rule ($\tau \neq 0$): If $e_1 = 0$ and $e_2 > 0$, then $\frac{\partial \bar{L}}{\partial e_1} < 0$ and $\frac{\partial \bar{L}}{\partial e_2} = 0$, such that MPE₁ < MPE₂. If $e_1 > 0$ and $e_2 = 0$, then $\frac{\partial \bar{L}}{\partial e_2} < 0$ and $\frac{\partial \bar{L}}{\partial e_1} = 0$, such that MPE₁ > MPE₂.

• If
$$e_1 > 0$$
 and $e_2 > 0$, then $\frac{\partial \bar{L}}{\partial e_1} = \frac{\partial \bar{L}}{\partial e_2} = 0$, such that MPE₁ =MPE₂.

The above rule states that fishermen will target the species that gives the higher MPE, or both species will be targeted if their MPEs are same. If $\lambda > 0$, the value of additional boat is positive and the fleet capacity constraint becomes binding; i.e., $e_i + e_{-i} = n$.

The optimal rule for $\tau = 0$, a special case, is slightly different from the above general rule. In this case only $\frac{\partial \bar{L}}{\partial e_1} = \frac{\partial \bar{L}}{\partial e_2} = 0$ can be satisfied, hence $e_i > 0, i = 1, 2$. Any effort allocation satisfying the fleet capacity constraint will be optimal, because every unit of ⁵⁹³ effort is equally divided between two species. We consider $\tau = 0$ as a trivial case, hence ⁵⁹⁴ the subsequent discussion will focus on the cases when $\tau > 0$.